

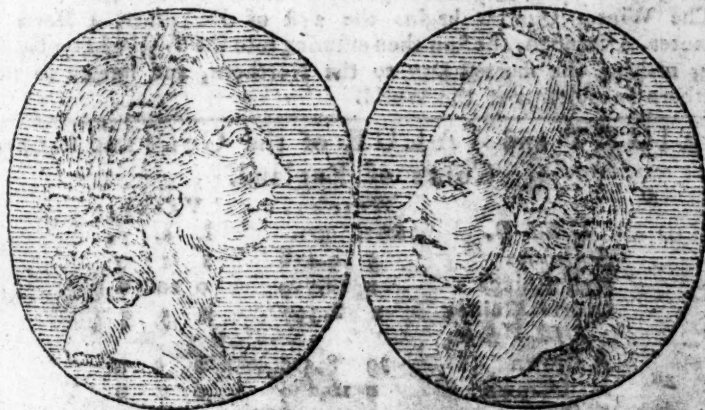
THE *P.P. 2nd 5 d.*
LADIES and GENTLEMENS
D I A R Y,
O R,
ROYAL ALMANACK;

For the Year of our LORD, 1778 :
Being the Second after Bissextile, or Leap Year.

CONTAINING,
Besides the CALENDAR, a great Variety of *Anigmas*,
Rebusies, Mathematical Solutions, &c. &c.

By REUBEN BURROW,

Late Assistant Astronomer at the Royal Observatory,
and Teacher of the Mathematics.



L O N D O N :

Printed for T. CARNAN, in St. Paul's Church Yard, who dispossessed
the Stationers Company of the exclusive Privilege of Printing
Almanacks, which they had unjustly monopolized 170 Years.



ECLIPSES in 1778.

In the course of this year there will be Three Eclipses, Two of the Sun, and One of the Moon, which will happen in the following Order: The First will be a visible Eclipse of the Sun on the 24th day of June in the Afternoon, the beginning at Forty-One Minutes after Three; Middle at Thirty-Five Minutes after Four; and the end at Twenty-Seven Minutes after Five, apparent time: The Digits eclipsed $6\frac{1}{2}$ on the Southern limb of the Sun: The Second is a visible Eclipse of the Moon on the 4th day of December in the Morning; the beginning at Twenty-Four Minutes after Four, Middle at Thirty-Seven Minutes after Five, and the End at Forty-Nine Minutes after Six, apparent time; the Digits eclipsed $6\frac{1}{2}$ on the Moon's Northern limb. The Third and Last is an invisible Eclipse of the Sun on the 18th of December, about Ten at Night.

COMMON NOTES, 1778.

Golden Number	-	-	12	Dominical Letter	-	-	D
Cycle of the Sun	-	-	23	Roman Indiction	-	-	11
Epact	-	-	1	Number of Direction	-	-	29

The FOUR QUARTERS of the YEAR.

The Spring Quarter begins this Year the 20th of March, at 10 Minutes after Noon, at which time the Sun enters the *Equinoctial Sign Aries*, making equal Day and Night all the World over.

The Summer Quarter commences the 21st Day of June, at 10 Hours 24 Minutes, Forenoon, the Sun then entering into the *Sign Cancer*, making the longest Day to all the Northern, and the shortest to all the Southern Parts of the World.

The Autumnal Quarter begins the 22d Day of September, at 11 Hours 47 Minutes at Night, at which Time the Sun enters *Libra*, making again equal Day and Night to all Parts of the World.

The Winter Quarter begins the 21st of December, 4 Hours 5 Minutes, Afternoon, the Sun then entering into the *Tropical Sign Capricorn*, making the shortest Day to the Northern, and longest to the Southern Inhabitants of the World.

WEIGHT and VALUE of the GOLD and SILVER COINS of England.

	WEIGHT.		VALUE.		
	dwt.	grs.	l.	s.	d.
GOLD.					
A Guinea	5	9,438	1	1	0
Half Guinea	2	16,719	0	10	6
Quarter Guinea	1	8,359	0	5	3
SILVER.					
A Crown	19	8,519	0	5	0
Half Crown	9	16,259	0	2	6
Shilling	3	20,903	0	1	0
Sixpence	1	22,451	0	0	6

Current Gold Coin must weigh as follows :

	dwt.	grs.
Guineas	5	8
Half Guineas	2	16
Quarter Guineas	1	8

First Quarter 6 day 8 h. 33 m. morning
 Full Moon 13 day 1 h. 33 m. morning
 Last Quarter 20 day 1 h. 19 m. afternoon
 New Moon 28 day 2 h. 46 m. afternoon

Sun enters Aquarius
 19d. 8h. 46m.
 Apparent time.

1	Th	Circumcision	8	5	3	55	22	59	6	A	34	4
2	F	Venus rises 6. 38 m.	8	4	3	56	22	54	7	44	5	
3	S		8	3	3	57	22	48	9	0	6	
4	D	2 S. aft. Christ.	8	2	3	58	22	42	10	16	7	
5	M	Old Christmas Day	8	1	3	59	22	35	11	35	8	
6	Tu	Epiphany. Twelfth Day	8	1	3	59	22	28	Morn.		9	
7	W	Julianus	8	0	4	0	22	20	0	55	10	
8	Th	Lucian	7	59	4	1	22	12	2	15	11	
9	F	Aldebaran, So. 8. 57	7	58	4	2	22	3	3	38	12	
10	S		7	57	4	3	21	54	4	59	13	
11	D	1 S. aft. Epip.	7	56	4	4	21	45	6	16	14	
12	M	Plow Mond. O. N. Y. d.	7	55	4	5	21	35	D rises		15	
13	Tu	Hilary. Camb. T. b.	7	54	4	6	21	25	4	a	39	16
14	W	Oxford Term begins	7	53	4	7	21	14	5	55	17	
15	Th	Exchequer opens	7	51	4	9	21	3	7	12	18	
16	F	Jupiter rises 6. 35 A.	7	50	4	10	20	52	8	25	19	
17	S	Old Twelfth Day.	7	49	4	11	20	40	9	36	20	
18	D	2 S. aft. Epip. Prisca.	7	48	4	12	20	28	10	44	21	
19	M	Q. Charl. birth-day kept	7	46	4	14	20	15	11	53	22	
20	Tu	Fabian B. & M. In 8 d. Hil.	7	45	4	15	20	2	Morn.		23	
21	W	Agnes [1 Ret.	7	44	4	16	19	49	1	0	24	
22	Th	Vincent	7	42	4	18	19	35	2	5	25	
23	F	Hilary Term begins	7	41	4	19	19	21	3	13	26	
24	S		7	39	4	21	19	6	4	17	27	
25	D	3 S. aft. Ep. Co. St. Paul	7	38	4	22	18	52	5	20	28	
26	M	Saturn rises 1. 35 M.	7	36	4	24	18	37	6	18	29	
27	Tu	Fr. A. Fr. b. From Hil. in	7	35	4	25	18	21	7	7	30	
28	W	Sirius So. 9. 48. [15 d. 2 Ret	7	33	4	27	18	5	D sets		1	
29	Th		7	31	4	29	17	49	5	a	24	2
30	F	K. Char. I. Martyr.	7	30	4	30	17	33	6	40	3	
31	S		7	28	4	32	17	16	7	57	4	

Days	L. of D.	Days inc	D. breaks	Sun East	Tw. ends	Cl. bef. S.	7 Stars So.
1	7 51	0 7	5 59	4 41	6 1	4 15	8 A 45
6	7 58	0 14	5 56	4 43	6 4	6 32	8 23
11	8 8	0 24	5 53	4 46	6 7	8 36	8 1
16	8 20	0 36	5 48	4 50	6 12	10 24	7 40
21	8 32	0 48	5 43	4 54	6 17	11 55	7 19
26	8 48	1 4	5 37	4 58	6 23	13 7	6 58

First Quarter 4 day 4 h. 37 m. afternoon

Full Moon 11 day 2 h. 46 m. afternoon

Last Quarter 19 day 10 h. 45 m. night

New Moon 27 day 4 h. 47 m. morning

Sun enters Pisces.

17d. 23h. 39m.

Apparent time.

D	M	DW	Sundays, Holidays, &c.	Sun rises	Sun sets	Sun. decl. S.	D rises & sets	D's age
1	D		4 S. aft. Epiphany	7 26	4 34	16 59	9 A 10	5
2	M		Purif. V. Mary. Candle. d.	7 25	4 35	16 41	10 34	6
3	Tu		Blase. Mor. Purif. 3 Ret.	7 23	4 37	16 24	11 55	7
4	W			7 21	4 39	16 6	Morn.	8
5	Th		Agatha	7 19	4 41	15 48	1 17	9
6	F			7 18	4 42	15 29	2 37	10
7	S		Venus rises 6. 59 M.	7 16	4 44	15 10	3 53	11
8	D		5 S. aft. Epip.	7 14	4 46	14 51	5 4	12
9	M		In 8 days of Pur. 4 Ret.	7 12	4 48	14 32	6 6	13
10	Tu		Capella South 7. 22	7 10	4 50	14 13	6 49	14
11	W			7 9	4 51	13 53	D rises	15
12	Th		Hilary Term ends	7 7	4 53	13 33	5 a 57	16
13	F		Old Candlemas day	7 5	4 55	13 13	7 10	17
14	S		Valentine	7 3	4 57	12 52	8 23	18
15	D		Septuagesima Sunday	7 1	4 59	12 32	9 31	19
16	M			6 59	5 1	12 11	10 41	20
17	Tu			6 57	5 3	11 50	11 49	21
18	W		Capella South 6. 51	6 56	5 4	11 29	Morn.	22
19	Th		Mars sets 7. 31 A.	6 54	5 6	11 7	0 57	23
20	F		Sirius South 8. 18	6 52	5 8	10 46	2 3	24
21	S			6 50	5 10	10 24	3 6	25
22	D		Sexagesima Sunday	6 48	5 12	10 2	4 5	26
23	M			6 46	5 14	9 40	4 58	27
24	Tu		S. Matth. P. Ad. Fr. born	6 44	5 16	9 18	5 44	28
25	W		Camb. Term divides m.	6 42	5 18	8 56	6 22	29
26	Th		Saturn rises 11. 26 Nig.	6 40	5 20	8 33	D sets	1
27	F		Aldebaran So. 5. 39	6 38	5 22	8 11	5 a 40	2
28	S		Hare hunting goes out	6 36	5 24	7 48	7 0	3

Days.	L. of D.	Days inc.	D. breaks	Sun East.	Tw. end.	Cl. bet S	7 Stars.
1	9 7	1 23	5 29	5 4	6 31	14 8	6 A 33
6	9 24	1 40	5 21	5 9	6 39	14 34	6 13
11	9 43	1 59	5 13	5 15	6 47	14 41	5 53
16	10 2	2 18	5 5	5 22	6 55	14 28	5 34
21	10 20	2 36	4 56	5 26	7 4	13 58	5 14
26	10 40	2 56	4 47	5 33	7 13	13 12	4 55

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March hath XXXI Days.

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First Quarter 6 day 0 h. 5 m. morning

Full Moon 13 day 5 h. 6 m. morning

Last Quarter 21 day 7 h. 15 m. morning

New Moon 28 day 4 h. 0 m. afternoon

S. enters Aries.

20d. 0h. 10m.

Apparent time.

1	D	Shrove Sunday. David	6	34	5	26	7	25	8 A 22	4
2	M	Chad.	6	32	5	28	7	3	9 45	5
3	Tu	Shrove Tuesday	6	30	5	30	6	40	11 7	6
4	W	Ash Wednesday	6	28	5	32	6	17	Morn.	7
5	Th		6	26	5	34	5	53	0 30	8
6	F		6	24	5	36	5	30	1 47	9
7	S	Perpetua	6	22	5	38	5	7	3 1	10
8	D	1 Sunday in Lent	6	20	5	40	4	43	4 2	11
9	M	Mars sets 7. 39 Af.	6	18	5	42	4	20	4 51	12
10	Tu	Procyon South 8. 4	6	16	5	44	3	57	5 27	13
11	W	Ember Week	6	14	5	46	3	33	5 57	14
12	Th	Gregory M.	6	12	5	48	3	9	D rises	15
13	F		6	10	5	50	2	46	6 A 8	16
14	S	Sirius So. 6. 56	6	8	5	52	2	22	7 21	17
15	D	2 Sunday in Lent	6	6	5	54	1	59	8 30	18
16	M		6	4	5	56	1	35	9 39	19
17	Tu	St. Patrick	6	2	5	58	1	11	10 48	20
18	W	Edward K. W. S.	6	0	6	0	0	48	11 55	21
19	Th	Jupiter South 9 24 N.	5	59	6	1	0	24	Morn.	22
20	F	Equal Day and Night	5	57	6	3	0	0	1 0	23
21	S	Benedict Abbot.	5	55	6	5	N	24	2 3	24
22	D	3 Sunday in Lent	5	53	6	7	0	47	2 57	25
23	M		5	51	6	9	1	11	3 43	26
24	Tu		5	49	6	11	1	34	4 24	27
25	W	Lady-Day, or Annun.	5	47	6	13	1	58	4 56	28
26	Th	Saturn rises 7. 16	5	45	6	15	2	21	5 24	29
27	F	Sirius So. 6. 9	5	43	6	17	2	45	5 48	30
28	S		5	41	6	19	3	8	D sets	1
29	D	4 S. in Lent. Mid-Lent S.	5	39	6	21	3	32	7 A 29	2
30	M		5	37	6	23	3	55	8 56	3
31	Tu		5	35	6	25	4	18	10 21	4

Days	L. of D.	Days inc.	D breaks	Sun	East	lw. ends	Cl. bef. S.	7 Stars So.
1	10 52	3 8	4 41	5 36	7 19	12 38	4 A 44	
6	11 12	3 28	4 31	5 42	7 29	11 30	4 26	
11	11 31	3 47	4 21	5 49	7 39	10 13	4 7	
16	11 51	4 7	4 10	5 55	7 50	8 47	3 49	
21	12 10	4 26	3 59	6 2	8 1	7 16	3 31	
26	12 30	4 46	3 47	6 8	8 13	5 43	3 13	

First Quarter	4 day	7 h. 50 m. morning	Sun enters Taurus. 19d. 13h. 2m. Apparent time.
Full Moon	11 day	8 h. 21 m. afternoon	
Last Quarter	20 day	0 h. 54 m. afternoon	
New Moon	27 day	0 h. 59 m. morning	

1	W		5	33	6	27	4	41	11	A	43	5
2	Th	Sirius So. 5. 51	5	31	6	29	5	4		Morn.		6
3	F	R. Bishop Chichester	5	29	6	31	5	27	1	1		7
4	S	St. Ambrose	5	27	6	33	5	50	2	7		8
5	D	5 S. in Lent. Old Lady-day	5	25	6	35	6	13	2	58		9
6	M		5	23	6	37	6	36	3	40		10
7	Tu	Mars sets 8. 1 N.	5	21	6	39	6	58	4	12		11
8	W		5	19	6	41	7	21	4	39		12
9	Th		5	17	6	43	7	43	4	58		13
10	F	Camb. Term ends	5	15	6	45	8	5	5	15		14
11	S	Oxf. Term ends	5	13	6	47	8	27	5	33		15
12	D	Palm Sunday	5	11	6	49	8	49		D rises		16
13	M	Jupiter So. 7. 50 A.	5	9	6	51	9	11	7	A	34	17
14	Tu	Regulus So. 8. 24	5	8	6	52	9	32	8	43		18
15	W	Clock with Sun	5	6	6	54	9	54	9	50		19
16	Th	Maund. Thursday	5	4	6	56	10	15	10	57		20
17	F	Good Friday	5	2	6	58	10	36		Morn.		21
18	S		5	0	7	0	10	57	0	58		22
19	D	Easter Sunday. <i>Alphege</i>	4	58	7	2	11	18	1	48		23
20	M	Easter Monday	4	56	7	4	11	39	2	30		24
21	Tu	Easter Tuesday	4	54	7	6	11	59	3	5		25
22	W		4	53	7	7	12	19	3	33		26
23	Th	St. George	4	51	7	9	12	39	3	57		27
24	F	Saturn So. 34m. aft. mid.	4	49	7	11	12	59	4	19		28
25	S	St. Mark. Prs. Mary born	4	47	7	13	13	18	4	37		29
26	D	1 S. after Easter. Low S.	4	45	7	15	13	38		D sets		1
27	M	Victory of Culloden	4	43	7	17	13	57	7	A	58	2
28	Tu		4	42	7	18	14	16	9	26		3
29	W	Oxf. and Camb. T. beg.	4	40	7	20	14	35	10	52		4
30	Th	Regulus So. 7. 24	4	38	7	22	14	53		Morn.		5

Days	D. of D.	Days inc.	D. breaks	Sun East	Tw. ends	Cl. bef. S.	Stars be.
1	12 54	5 10	3 32	6 15	8 28	3 53	2 A 51
6	13 14	5 30	3 19	6 21	8 41	2 23	2 33
11	13 33	5 49	3 6	6 27	8 54	0 57	2 14
16	13 51	6 7	2 52	6 33	9 8	0 A 21	1 56
21	14 11	6 27	2 37	6 39	9 23	1 29	1 37
26	14 30	6 46	2 22	6 45	9 38	2 26	1 17

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May hath XXXI Days.

7

First Quarter 3 day 4 h. 28 m. afternoon

Full Moon 11 day 0 h. 7 m. afternoon

Last Quarter 19 day 2 h. 37 m. afternoon

New Moon 26 day 8 h. 34 m. morning

Sun enters Gemini.

20d. 13h. 42m.

Apparent time.

1	F	St. Philip and James	4	36	7	24	15	11	0	M	4	6
2	S		4	35	7	25	15	29	1		2	7
3	D	2 S. aft. East. Inv. of Crofs	4	33	7	27	15	47	1		49	8
4	M	From East. In 15 days	4	31	7	29	16	4	2		23	9
5	Tu	Spica South 10. 17 [Ret.	4	29	7	31	16	21	2		49	10
6	W	John E. P. Lat. E. Ter. b	4	28	7	32	16	38	3		10	11
7	Th	Venus sets 8. 39 A	4	26	7	34	16	55	3		29	12
8	F	Regulus So. 6. 54	4	24	7	36	17	11	3		46	13
9	S		4	23	7	37	17	27	4		2	14
10	D	3 S. after Easter	4	21	7	39	17	43	4		18	15
11	M	From East. in 3 weeks	4	20	7	40	17	58				16
12	Tu	Old May day. [Ret.	4	18	7	42	18	14	8	A	48	17
13	W	Jupiter sets 1. 33 M	4	17	7	43	18	28	9		52	18
14	Th		4	15	7	45	18	43	10		54	19
15	F	Arcturus South 10 34	4	14	7	46	18	57	11		49	20
16	S		4	12	7	48	19	11				21
17	D	4 S. after Easter	4	11	7	49	19	25	0		31	22
18	M	From East. in 1 mo. 3 Ret	4	9	7	51	19	38	1		8	23
19	Tu	Q. Cha. b. 1744 Dunst.	4	8	7	52	19	51	1		38	24
20	W	Saturn So. 10. 45 N	4	7	7	53	20	3	2		3	25
21	Th		4	5	7	55	20	16	2		24	26
22	F	Prs. Eliz. born 1770	4	4	7	56	20	28	2		43	27
23	S		4	3	7	57	20	39	3		3	28
24	D	Rogation Sunday	4	1	7	59	20	50	3		22	29
25	M	From East. in 5 weeks	4	0	8	0	21	1	3		48	1
26	Tu	Augustin. All twil. [Ret.	3	59	8	1	21	12				2
27	W	Venerable Bede	3	58	8	2	21	22	8	A	22	3
28	Th	Ascensf. day. Holy Thurs	3	57	8	3	21	32	9		42	4
29	F	K. Ch. II. Rest. On the	3	56	8	4	21	41	10		52	5
30	S	[mor. of Ascensf. 5 Ret.	3	55	8	5	21	50	11		44	6
31	D	Sunday after Ascension	3	54	8	6	21	59				7

Days	L. or L.		Days In.	D. breaks	Sun East	Tw. ends	Cl. aft. S.	7 Stars So.
1	14	47	7 3	2 5	6 50	9 55	3 10	1 A 0
6	15	5	7 21	1 47	6 55	10 13	3 41	0 40
11	15	21	7 37	1 26	7 0	10 34	3 58	0 21
16	15	36	7 52	1 6	7 4	10 54	4 2	0 1
21	15	50	8 6	0 27	7 8	11 33	3 50	11 M 41
26	16	2	8 18	NoNight	7 12	NoNight	3 25	11 23

First Quarter	2 day	2 h. 34 m. morning	
Full Moon	10 day	3 h. 50 m. morning	S. enters Cancer.
Last Quarter	18 day	0 h. 25 m. morning	20d. 22h. 24m.
New Moon	24 day	3 h. 37 m. afternoon	Apparent time.

1	N	Nicomede.	Term ends	3	53	8	7	22	7	0	M	53	8
2	T			3	52	8	8	22	15	1		16	9
3	W	Camb. Term divid.	[ends	3	51	8	9	22	22	1		36	10
4	Th	K. G. III. b. 1738	Ox. T	3	50	8	10	22	29	1		51	11
5	F	Pr. Er. Aug. b. Boniface		3	49	8	11	22	36	2		9	12
6	S	Arcturus South 9. 6		3	48	8	11	22	42	2		29	13
7	D	Whit-Sunday		3	48	8	12	22	48	2		42	14
8	M	Whit-Monday		3	47	8	13	22	54	3		3	15
9	Tu	Whit-Tuesday		3	47	8	13	22	59	3		25	16
10	W	Prs. Amel. b. 1738	Em. Week	3	46	8	14	23	3		D	rites	17
11	T	St. Barnabas		3	46	8	14	23	8	9	A	43	18
12	F			3	45	8	15	23	12	10		30	19
13	S	Venus sets 9. 55 N.		3	45	8	15	23	15	11		7	20
14	D	Trinity Sunday		3	44	8	16	23	18	11		39	21
15	M	Cl with S. On mor. H. Tr.		3	44	8	16	23	21		Morn.		22
16	Tu	Jupiter S. 4. rA	[1 Ret	3	44	8	16	23	23	0			23
17	W	St. Alban Ox. Term beg		3	43	8	17	23	25	0		25	24
18	Th	Corpus Christi.		3	43	8	17	23	26	0		44	25
19	F	Trinity Term begins		3	43	8	17	23	27	1		1	26
20	S	T. Edw. K. W. S.		3	43	8	17	23	28	1		20	27
21	D	1 S. aft. Trin. Long. day		3	43	8	17	23	28	1		42	28
22	M	In 8 days Holy Trin	2 Ret	3	43	8	17	23	28	2		7	29
23	Tu			3	43	8	17	23	27	2		40	30
24	W	St John Bap. Midsum day		3	43	8	17	23	26		D	fets	1
25	Th	Jupiter sets 10 49 N. [OE		3	43	8	17	23	25	9	A	27	2
26	F			3	44	8	16	23	23	10		9	3
27	S	Arcturus So. 7. 39		3	44	8	16	23	20	10		48	4
28	D	2 S aft. Trinity		3	44	8	16	23	18	11		15	5
29	M	St. Peter & Paul. In 15d.		3	45	8	15	23	15	11		35	6
30	Tu	[of H Trin. 3 Ret		3	45	8	15	23	11	11		53	7

Days	L. of D.	Days inc.	D. break	sun East	Tw. enus	Cl. art. S.	7 Stars So
1	16 15	8 31	No	7 15	No	2 38	10 M 57
6	16 23	8 39	constant	7 18	constant	1 49	10 36
11	16 29	8 45	real night, but	7 19	real night, but	0 53	10 16
16	16 33	8 49	twilight.	7 21	twilight.	bef. 9	9 55
21	16 34	8 50		7 21		1 14	9 34
26	16 33	dec. 2		7 21		2 18	9 13

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July hath XXXI Days.

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First Quarter 1 day 2 h. 48 m. afternoon
Full Moon 9 day 6 h. 46 m. afternoon
 Last Quarter 17 day 7 h. 43 m. morning
New Moon 23 day 11 h. 7 m. night
 First Quarter 31 day 5 h. 42 m. morning

Sun enters Leo.
 22d. 9h. 7m.
 Apparent time.

1	W	St. Marcial	3	46	8	14	23	7	Morn.	8
2	Th	Visit. B. V. M.	3	46	8	14	23	3	0	8
3	F	Dies Comitior.	3	47	8	13	22	58	0	25
4	S	Tran. St. Mart. P.	3	47	8	13	22	53	0	41
5	D	3 S. aft. Trin. O. Mid. d.	3	48	8	12	22	47	1	1
6	M	In 3 W. H. Trin. 4 Ret.	3	49	8	11	22	42	1	23
7	Tu	Cho a Becket Camb. Com.	3	49	8	11	22	35	1	51
8	W	Term ends	3	50	8	10	22	29	2	26
9	Th	Lyra South 11. 12	3	51	3	9	22	21	Drises	16
10	F	Camb. Term ends	3	52	3	8	22	14	9 A	3
11	S		3	53	3	7	22	6	9	36
12	D	4 S. aft. Trinity	3	54	3	6	21	58	10	5
13	M	Oxford Aft	3	55	8	5	21	49	10	24
14	Tu	Jupiter sets 9 37 N.	3	56	8	4	21	40	10	45
15	W	St. Swithin	3	57	3	3	21	31	11	5
16	Th		3	58	3	2	21	21	11	22
17	F	Autares So 8 27	3	59	3	1	21	11	11	42
18	S	Oxford Term ends	4	0	3	0	21	1	Morn.	25
19	D	5 S. aft. Trinity	4	1	7	59	20	50	0	4
20	M	Margaret V. and M.	4	3	7	57	20	39	0	32
21	Tu		4	4	7	56	20	27	1	6
22	W	St. Mary Magdalen	4	5	7	55	20	15	1	58
23	Th		4	7	7	53	20	3	D sets	1
24	F		4	8	7	52	19	50	8 A	41
25	S	St. James	4	9	7	51	19	38	9	10
26	D	6 S. aft. Trinity St. Anne	4	11	7	49	19	24	9	35
27	M	Saturn sets 11. 1 N.	4	12	7	48	19	11	9	55
28	Tu		4	14	7	46	18	57	10	12
29	W	Autares So 7 39	4	15	7	45	18	43	10	28
30	Th	Dog days begin	4	17	7	43	18	28	10	46
31	F		4	18	7	42	18	14	11	4

Days	h. of D.	Days de	D. breaks	Sun East	Tw. ends	Cl. bef. S.	7 S. ars So
1	16 29	0 5		7 19		3 19	8 M 53
6	16 22	0 12	No real	7 18	No real	4 13	8 32
11	16 14	0 20	Night.	7 15	Night.	4 58	8 11
16	16 4	0 30		7 12		5 32	7 51
21	15 52	0 42	0 7	7 9	11 53	5 54	7 31
26	15 37	0 57	0 51	7 5	11 3	6 2	7 11

Full Moon 8 day 8 h. 25 m. afternoon
 Last Quarter 15 day 1 h. 30 m. afternoon | Sun enters Virgo.
 New Moon 22 day 8 h. 4 m. morning | 22d. 15h. 28m.
 First Quarter 29 day 11 h. 14 m. night | Apparent time.

1	S	Lammas-day	4	20	7	40	17	59	11	A	24	10
2	D	7 Sund. aft. Trinity	4	21	7	39	17	43	11		50	11
3	M		4	23	7	37	17	28		Morn.		12
4	Tu		4	24	7	36	17	12	0		22	13
5	W	Lyra So. 9. 26.	4	26	7	34	16	55	1		3	14
6	Th	Transfiguration	4	28	7	32	16	39	1		54	15
7	F	Name of Jesus	4	29	7	31	16	22	2		54	16
8	S		4	31	7	29	16	5		D rises		17
9	D	8 S. aft. Trinity	4	33	7	27	15	48	8	A	33	18
10	M	St. Lawrence	4	35	7	25	15	30	8		53	19
11	Tu	Prs. Brunf. born 1737	4	36	7	24	15	13	9		11	20
12	W	Pr. of Wales bo. 1762 Old	4	38	7	22	14	55	9		28	21
13	Th	Mars ri. 2. 36m [Lam. d.]	4	40	7	20	14	36	9		48	22
14	F		4	41	7	19	14	18	10		9	23
15	S	Assumption Virgin Mary	4	43	7	17	13	59	10		35	24
16	D	9 S. aft. Trin. Pr Fred	4	45	7	15	13	40	11		8	25
17	M	[born 1763]	4	47	7	13	13	21	11		49	26
18	Tu		4	49	7	11	13	2		Morn.		27
19	W	Lyra South 8. 32	4	50	7	10	12	42	0		46	28
20	Th		4	52	7	8	12	22	1		56	29
21	F	Athanasius. Pr. Wm. Hen	4	54	7	6	12	2	3		12	1
22	S	[bo. 1763]	4	56	7	4	11	42		D sets		2
23	D	10 S. aft. Trinity	4	58	7	2	11	22	8	A	2	3
24	M	St. Bartholomew	5	0	7	0	11	1	8		20	4
25	Tu	Saturn sets 9. 13N	5	1	6	59	10	41	8		37	5
26	W		5	3	6	57	10	20	8		54	6
27	Th		5	5	6	55	9	59	9		11	7
28	F	St. Augustin	5	7	6	53	9	37	9		31	8
29	S	St. John Baptist beb.	5	9	6	51	9	16	9		56	9
30	D	11 S. aft. Trinity	5	11	6	49	8	55	10		25	10
31	M	Clock with Sun	5	13	6	47	8	33	11		3	11

Days	L. of D.	Days dec.	D. breaks	Sun East	Tw. ends	I. bet. S.	Stars So.
1	15 21	1 13	1 27	7 0	10 33	5 52	6 M 48
6	15 5	1 29	1 43	6 55	10 17	5 26	6 29
11	14 48	1 46	2 5	6 50	9 55	4 46	6 9
16	14 30	2 4	2 21	6 45	9 39	3 52	5 51
21	14 12	2 22	2 37	6 39	9 23	2 46	5 32
26	13 53	2 41	2 51	6 33	9 9	1 28	5 14

1778.

September hath XXX Days.

11

Full Moon 6 day 8 h. 43 m. afternoon
 Last Quarter 13 day 7 h. 9 m. afternoon Sun enters Libra.
 New Moon 20 day 7 h. 18 m. afternoon 22d. 11 h. 47 m.
 First Quarter 28 day 6 h. 32 m. afternoon Apparent time.

1	Tu	Giles	5	15	6	45	8	11	11 A 50	12
2	W	London burnt 1666 O S	5	17	6	43	7	49	Morn.	13
3	Th		5	19	6	41	7	27	0 47	14
4	F	Aquilæ So. 8. 46	5	20	6	40	7	5	1 52	15
5	S		5	22	6	38	6	43	3 4	16
6	D	12 S. aft. Trinity	5	24	6	36	6	20	Drises	17
7	M	Eunurchus. Dog-days E.	5	26	6	34	5	58	7 A 24	18
8	Tu	Nativity V. Mary	5	28	6	32	5	35	7 42	19
9	W	Venus sets 7. 42 N.	5	30	6	30	5	13	8 0	20
10	Th		5	32	6	28	4	50	8 22	21
11	F	Fomalhaut South 11 24	5	34	6	26	4	27	8 45	22
12	S		5	36	6	24	4	4	9 16	23
13	D	13 S. aft. Trinity	5	38	6	22	3	41	9 55	24
14	M		5	40	6	20	3	18	10 47	25
15	Tu		5	42	6	18	2	55	11 51	26
16	W	Ember Week	5	44	6	16	2	32	Morn.	27
17	Th	Lambert	5	46	6	14	2	8	1 2	28
18	F		5	48	6	12	1	45	2 24	29
19	S	Mars rises 2. 35 M	5	50	6	10	1	22	3 43	30
20	D	14 S. aft. Trinity	5	52	6	8	0	58	Drises	1
21	M	St. Matthew	5	54	6	6	0	35	6 A 50	2
22	Tu	K. Geo III. Cor. 1761.	5	56	6	4	0	12	7 7	3
23	W	[Equal Day & Night]	5	57	6	3	8	12	7 25	4
24	Th		5	59	6	1	0	35	7 42	5
25	F	Saturn sets 7. 27 N	6	1	5	59	0	59	8 6	6
26	S	St. Cyprian	6	3	5	57	1	22	8 31	7
27	D	15 S. aft. Trinity	6	5	5	55	1	46	9 7	8
28	M		6	7	5	53	2	10	9 49	9
29	Tu	St. Mich. Tr. R. L. Hare h	6	9	5	51	2	33	10 41	10
30	W	St. Jerome [comes in]	6	11	5	49	2	56	11 41	11

Days	L. of D.	Days dec.	D. breaks	Sun East	Tw. ends	Cl. aft. S.	7 Stars	10
1	13 31	3 3	3 8	6 26	8 52	0 18	4 M	52
6	13 11	3 23	3 21	6 20	8 39	1 55	4	34
11	12 52	3 42	3 34	6 14	8 26	3 37	4	16
16	12 32	4 2	3 46	6 8	8 14	5 22	3	58
21	12 13	4 21	3 57	6 2	8 3	7 6	3	40
26	11 53	4 41	4 9	5 56	7 51	8 48	3	22

Full Moon 6 day 8 h. 1 m. morning
 Last Quarter 13 day 1 h. 47 m. morning Sun enters Scorpio.
 New Moon 20 day 9 h. 30 m. morning 22d. 19h. 36m.
 First Quarter 28 day 2 h. 1 m. afternoon Apparent time.

1	Th	<i>Remigius</i>	5	13	5	47	3	19	Morn.	12
2	F		5	15	5	45	3	43	0	52
3	S	Fomalhaut South 10 6	5	17	5	43	4	6	2	5
4	D	16 S. aft. Trinity	5	19	5	41	4	29	3	24
5	M		5	21	5	39	4	52	4	44
6	Tu	<i>Faith</i>	5	23	5	37	5	15	D rises	17
7	W	Venus sets 6. 53 N	5	25	5	35	5	38	6 A	32
8	Th		5	27	5	33	6	1	6	57
9	F	<i>St. Denys</i>	5	29	5	31	6	24	7	26
10	S	<i>O. Mich. d. Oxf. & Cam</i>	5	31	5	29	6	47	8	1
11	D	17 S. aft. Tr. [Terms beg	5	33	5	27	7	10	8	50
12	M		5	35	5	25	7	32	9	49
13	Tu	<i>Tr. K. Ed. Confessor</i>	5	37	5	23	7	55	11	0
14	W	Mars rises 2. 34 M	5	39	5	21	8	17	Morn.	25
15	Th		5	41	5	19	8	40	0	15
16	F		5	43	5	17	9	2	1	35
17	S	<i>Ethelred Virg.</i>	5	45	5	15	9	24	2	5
18	D	18 S. aft. Trin. St. Luke	5	46	5	13	9	46	4	1
19	M		5	48	5	11	10	7	5	21
20	Tu		5	50	5	10	10	29	D sets	2
21	W		5	52	5	8	10	51	5 A	54
22	Th		5	54	5	6	11	12	6	14
23	F		5	56	5	4	11	33	6	39
24	S	[Access. <i>Gripi</i>	5	58	5	2	11	54	7	8
25	D	19 S. aft. Trin. K. Geo. III	7	0	5	0	12	15	7	4
26	M	K. Geo. III. Procl. 1760	7	1	5	59	12	35	8	35
27	Tu		7	3	5	57	12	56	9	31
28	W	St. Simon and Jude	7	5	5	55	13	16	10	39
29	Th		7	7	5	53	13	36	11	47
30	F	Fomalhaut South 8 24	7	9	5	51	13	56	Morn.	12
31	S		7	11	4	49	14	15	1	2

Days	L. of D	Days to	D. breaks	un. Eat	Tw. ena	Cl. aft. S	Stars Se							
1	11 33	5	1	4	20	5	49	7	40	10	25	3	M	4
6	11 14	5	20	4	30	5	43	7	30	11	56	2		45
11	10 54	5	40	4	40	5	37	7	20	13	16	2		27
16	10 35	5	59	4	49	5	31	7	11	14	24	2		8
21	10 16	6	18	4	59	5	25	7	2	15	17	1		50
26	9 57	6	37	5	7	5	10	6	53	15	53	1		31

Full Moon	4 day	0 h. 40 m.	afternoon	
Last Quarter	11 day	10 h. 26 m.	night	S. ent. Sagittarius
New Moon	19 day	2 h. 46 m.	morning	21 d. 15 h. 53 m.
First Quarter	27 day	7 h. 52 m.	morning	Apparent time.

1 D	20 S. aft. Trin. All Saints	7	12	4	48	14	34	2 M	19	14
2 M	Pr. Ed. bo. 1767 All Souls	7	14	4	46	14	53	3	39	15
3 Tu	Mor. of all Souls 1 Ret.	7	16	4	44	15	12	4	59	16
4 W		7	18	4	42	15	31	D	rises	17
5 Th	Powder Plot 1605. O. S.	7	20	4	40	15	49	5 A	25	18
6 F	Mich. Ter. beg Leonard.	7	21	4	39	16	7	6	c	19
7 S	Duke of Cumb. bo. 1745	7	23	4	37	16	25	6	43	20
8 D	21 S. aft. Tri. Prs. So. Au.	7	25	4	35	16	43	7	39	21
9 M	Ld. Mayor's d. [bo. 1768]	7	26	4	34	17	0	8	50	22
10 Tu		7	28	4	32	17	17	10	7	23
11 W	St. Martin	7	30	4	30	17	33	11	23	24
12 Th	Mor. of St. Mart. 2 Ret.	7	31	4	29	17	50	morn.		25
13 F	Britius. Venus sets 6 42 A	7	33	4	27	18	6	0	44	26
14 S		7	35	4	25	18	21	1	57	27
15 D	22 S. aft. Trin. Machutu	7	36	4	24	19	37	3	10	28
16 M		7	38	4	22	18	52	4	22	29
17 Tu	Hugh B. Lincoln	7	39	4	21	19	7	5	32	30
18 W	In 8 days of St. Mar. 3 Ret.	7	41	4	19	19	21	6	42	1
19 Th	Mars rises 2. 15 M	7	42	4	18	19	35	D	fets	2
20 F	Edm. K. and Mart.	7	44	4	16	19	49	5 A	6	3
21 S	Fomalhaut So. 6. 56	7	45	4	15	20	2	5	41	4
22 D	23 S. aft. Trin. Cecilia.	7	46	4	14	20	15	6	24	5
23 M	Clement	7	48	4	12	20	27	7	19	6
24 Tu		7	49	4	11	20	40	8	19	7
25 W	D. of Glo. bo. 1743 Catl	7	50	4	10	20	51	9	27	8
26 Th	[in 15 d of S. Mart. 4 Ret]	7	51	4	9	21	3	10	38	9
27 F		7	53	4	7	21	14	11	52	10
28 S	Michaelm. Term ends	7	54	4	6	21	25	morn.		11
29 D	Advent Sunday	7	55	4	5	21	34	1	7	12
30 M	St. Andrew	7	56	4	4	21	45	2	23	13

Days.	h. of D.	Days of	D. breaks	Sun East.	Tw. end	Cl. fr. s.	Stars So.
1	9	35	6	59	5	17	5 12 6 43 16 12 1 M 7
6	9	20	7	14	5	25	5 7 6 35 16 7 0 47
11	9	1	7	33	5	32	5 2 6 28 15 41 0 27
16	8	45	7	49	5	38	4 57 6 22 14 53 0 7
21	8	30	8	4	5	44	4 53 6 16 13 43 11 A 46
26	8	17	8	17	5	40	4 40 6 11 12 14 11 25

Full Moon	4 day	5 h. 29 m. morn.	
Last Quarter	10 day	9 h. 48 m. night	S. ent. Capricorn
New Moon	18 day	10 h. 4 m. night	21 d. 4h. 5m.
First Quarter	26 day	11 h. 9 m. night	Apparent time.

1	Tu		7	57	4	3	21	54	3	M	43	14
2	W	Fomalhaut So. 6. 9	7	58	4	2	22	3	5		10	15
3	Th		7	59	4	1	22	11	D	rises		16
4	F	Barbara. Moon eclipsed	8	0	4	0	22	19	4	A	24	17
5	S		8	1	3	59	22	27	5		15	18
6	D	2 S. in Advent Nicholas	8	2	3	58	22	34	6		21	19
7	M	Venus sets 6. 33 A	8	2	3	58	22	41	7		39	20
8	Tu	Conception Virgin Mary	8	3	3	57	22	47	8		59	21
9	W		8	4	3	56	22	53	10		19	22
10	Th		8	4	3	56	22	59	11		37	23
11	F		8	5	3	55	23	4		morn.		24
12	S		8	6	3	54	23	8	0		52	25
13	D	3 S. in Advent Lucy	8	6	3	54	23	12	2		3	26
14	M	Mars rises 1. 45 m	8	6	3	54	23	16	3		12	27
15	Tu	[Em. W.]	8	7	3	53	23	19	4		23	28
16	W	O. Sap. Camb Ter. ends.	8	7	3	53	23	22	5		31	29
17	Th	Oxford Term ends	8	7	3	53	23	24	6		39	30
18	F	Sun eclipsed	8	7	3	53	23	26	D	fets		1
19	S		8	8	3	52	23	27	4	a	11	2
20	D	4 S. in Advent	8	8	3	52	23	28	5		2	3
21	M	St. Thomas. Shortest day	8	8	3	52	23	28	6		0	4
22	Tu		8	8	3	52	23	28	7		6	5
23	W		8	8	3	52	23	27	8		13	6
24	Th	Sun and clocks together	8	8	3	52	23	26	9		26	7
25	F	Christmas Day	8	7	3	53	23	25	10		37	8
26	S	St. Stephen	8	7	3	53	23	23	11		51	9
27	D	1 S. after Christ. St John	8	7	3	53	23	20		morn.		10
28	M	Innocents	8	7	3	53	23	17	1		6	11
29	Tu	Fox Hunting comes in	8	6	3	54	23	14	2		26	12
30	W		8	6	3	54	23	10	3		49	13
31	Th	Silvester	8	5	3	55	23	5	5		13	14

Days.	L. of D.	Day dec.	D. breaks	Sun East.	1 w. ends	1. art S.	7	Scars	30.
1	8	6	8 28	5 54	4 45	6 6	10 28	11 A	3
6	7	57	8 37	5 57	4 43	6 3	8 26	10	41
11	7	50	8 44	5 59	4 41	6 0	6 11	10	19
16	7	46	8 48	6 1	4 40	5 59	3 41	9	57
21	7	44	8 50	6 1	4 39	5 59	1 17	9	35
26	7	46	Incr. 2	6 1	4 40	5 59	1 ber 3	9	13

ANSWERS to the QUERIES, REBUSES, &c. in Last Year's DIARY.

Query I. Answered by Mr. Joseph James, of Stoke-Bishop, near Bristol.

A Body will keep longer in moist ground than in dry, because in the former case the air is more excluded than in the latter.

Query II. Answered by Caput Mortuum.

I believe, experience teaches that when children begin to make use of their hands, both are used indifferently, which perhaps would be the case when grown did they remain in a state of Nature.—The preference given to the right-hand was certainly owing to *custom*, for it does not seem to depend on the predominancy of any *natural* impulse.

Query III. Answered by Mr. I. Dalby, (the Proposer).

It has been a matter of dispute among optical writers, whether an object when viewed through a magnifying lens appears farther off, or nearer, than when viewed with the naked eye; but the following experiments, I think, will clear up the point.

I. Bring a small object nearer the eye than the limits of distinct vision, then if a lens of a sufficient magnifying power be properly placed between the eye and object it will be seen distinctly;—here it is evident that it *seems* farther off now viewed through the lens, for before we thought, and which was true in fact, that it was too near.

II. Take the tube of a common refracting telescope, or any other tube in one end of which is fixed a magnifying lens, through this look at the inside of the tube and it will appear wider and longer according to the magnifying power of the lens: And the reason is this,—every object seen distinctly through the lens is magnified in length as well as breadth, and therefore a small object placed in the tube must seem farther off than it would at the same distance if viewed with the naked eye, consequently, in any case, if we consider the space between the glass and object as a tube, this experiment sufficiently determines the matter in question.

Hence, it follows, that the parts of an object when seen through a magnifying lens, cannot appear, with respect to each other, in their natural situation.

Query IV. Answered by Mr. Thomas Hatton.

When a body moves upon rollers the diameters of the rollers become as perpetual *radii* to the body moved, and the motion of the body is as those *radii*; but the motion of the rollers is as their perpetual *radii*, therefore, as the former *radii* are double of the latter, the motion produced from them must be so too.

Query V. in the Diary for 1776. Answered by Mr. I. Dalby.

Perhaps it is impossible to determine who was the inventor of Pocket Watches, but it is certain they were in use before the time of Hooke or Huygens. We learn from *Twelfth-night*, Act 2. where Malvolio talks of winding up his watch, that they were worn in *Shakespeare's* time; and we are told in *Stow's Chronicle* that a watch was found upon Guy

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Guy Fawkes when detected in the powder-plot: this the Conspirators bought the day before to determine how long the touchwood would burn before it kindled the gunpowder.—In the English *Orlando Furioso*, Fol. 1591. there is a print of the translator Sir *John Harrington*, with a watch before him on a table; near the hour of 12 a ring is fixed to the case, and another on the opposite side to which is tyed a string with a key at the end, like that of a modern watch.

But before that time, if history can be credited, watch-work was brought to great perfection, for we are informed by *Lonicerus* in *Hondorfi Theatrum Historicum*, that the Emperor *Charles V.* had a watch of curious workmanship; this he once lost in a croud, but it striking the hour of the day in the thief's pocket alarmed him in such a manner that he immediately confessed the theft:—probably this watch was made by *Jannellus Turrianus*, who used to divert the Emperor in his solitude with various mechanical devices, and, on account of his ingenuity, was called the *Archimedes* of his time.

Hooke seems to have been the first that regulated the ballance by means of a spring; tho' the invention was afterwards claimed by the *Abbé de Hautefeuille*.

Since the above, we have received the following from Mr. Tho. Hatton, Watch and Gold Scale-maker in the Old Bailey, London.

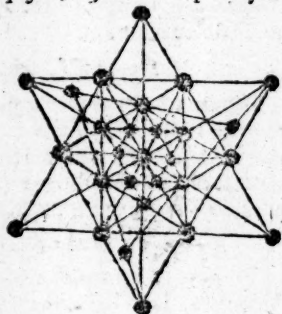
A few years ago there was found among the ruins of Bruce-Castle in Scotland a pocket watch, not of the largest size; on the dial, which is of silver, there are the words, *Robertus B. Rex Scottorum*, and on the upper plate where Watchmakers put their names, *Johann. Creitt. Mayr.* both engraven in the Old English letter; when it was found it had a piece of fine transparent horn instead of a glass. I have examined it in pieces and cannot find that it differs in the construction from the watches made in *Huygens's* time before the spring was applied to the ballance, having a fine catgut, a spiral spring, and two arms to the ballance, like those old watches, many of which I have mended.

If the engraving is not an imposition, it is certainly very old, as *Robert Bruce* died in 1328.—At present it is in the hands of an Antiquarian, and is look'd upon as a great curiosity.

Answer to the Paradox, with a new one proposed, by David ap Rhys.

To the Proposer.

In the margin's a plan, Sir,
Your purpose will answer.
Now shew, if you can, Sir,
(As you are a man, Sir,)
How in rows I can fix
Some twenty-four leeks;
But first, you must know,
I'd have four in each row,
On lines that are streight,
And just twenty-eight.



REBUS I, Answered by Miss Lackit, addressed to the Proposer.

Sir, Are you a youth or a cunning old stager,
It matters not which, I'll my maidenhead wager,

That

Answers to Queries, Rebusses, &c. 17

That young *Lucy Lackit*'s as handsome and sweet
As your fairest of fairs, although she's *Miss Keet*.

All the Rebusses answered by Captain Flash.

Pox take all the whores, and the peace which is worse, II.
I'm ruin'd in carcase as well as in purse,
No *Bagnigg-wells* rake ever look'd half so thin, III.
Tho' exhausted to nothing but bones and the skin;
At Almack's such cursed ill-luck too I meet,
So, must starve 'till the wars,—or else marry *Miss Keet*. I.

ANSWERS to the ENIGMAS in last Year's DIARY.

- | | |
|-------------|-----------------------|
| I. A Flame | IV. A Windmill |
| II. Content | V. Parchment |
| III. A Fox | Prize. A Close-stool. |

The Prize Enigma answered by Miss Lee.

The prize, if I guess right, is *close-stool* or pot;
So I hope the ten Diaries will fall to my lot.

The same answered by Mr. Thomas Hoy.

Hodge, when by the fire, the Riddles read o'er,
Swore the prize could be nothing but some common-shore;
Says Nell, take a large dose of jalap, you fool,
And I'll warrant 'twill put you in mind of *close-stool*.

The same answered by Mr. Joseph James.

When Limberham one night would clamber
Four stories up to Cloe's chamber,
Eager, and groping in the dark,
The aged, feeble, am'rous spark
O'er three-leg'd chair, O foul disgrace!
Fell prone and broke the *sacred vase*—
Said Cloe, you old fumbling fool,
Could not your worship smell *close-stool*?

All the Enigmas answered by Mr. Leonard Walker.

Enigma the first I am sure is a *flame*;
The second, I think, we may *bappiness*'s name;
The third is a *fox*, sans confusion or doubt;
The fourth is a *windmill* most clearly made out;
The fifth must be *parchment* to bind knave and fool;
And Dalby's *sweet prize*, a capacious *close-stool*.

A general answer to the Rebusses and Enigmas by Mr. Dalby.

Says Dick to his wife, thou'rt the plague of my life,

I wish longer single I'd tarry'd;
Or before I had led such a scold to my bed,
That unto *Miss Keet* I'd been marry'd.

Pox take ye, says Kate, when it was my fate

To be taken, for better, for worse,
Tho' you were undeserving, I kept you from starving,
And with money replenish'd your purse;

I. Reb.

II.

B

Hence

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Hence I did not suspect you'd your duty neglect,
 But each night you lie still,—snoring drunk,
 Yet shew yourself stout at a *Bagnigge-wells* rout, III.
 When regaling with some dirty punk.
 Thus, you idle sot, 'twixt a wh—e and the pot,
 Divide all the cash you can handle ;---
 Your tongue's very quick,---but no more, reply'd Dick,
 Lest your Tete meets the *flame* of this candle. I. *Enig.*
 Quoth she, who's *content* always to keep Lent ?--- II.
 But tho' you were cunning as *fox*, III.
 It may be the fate of your *windmill*-like pate IV.
 To look more like that of an ox.
 I shall not be horn'd *gratis*, my dear *nunquam satis*,
 Quoth Dick, for before I'm that fool,
 This Calamus Rotang shall your *parchment* hide bang V.
 'Till the floor you mistake for *close-shool*. Prize.

The TOBACCO-SMOKERS; Being an Answer to all the Enigmas, by Dr. SLOP.

Companions, *Harry*, *Ned*, and *Will*,
 One evening met to smoke their fill,
 To laugh and tell a merry tale,
 And bumpers quaff of nappy ale ;
Harry, who used to smoke and drink,
 Could do it easily as think,
 And *Ned* at times would burn the weed
 Either for company or need ;
 But *Will* had little used either,
 And therefore master was of neither,
 Yet now he was resolv'd to try,
 As we shall shew you by and by.
 Pipes and tobacco soon were plac'd
 Before 'em, and the table grac'd
 With *candles*, matches,---all things fit, I.
 And *singo quantum sufficit*,
 Brew'd just three years ago come Lent,
 Such any toper would content ; II.
Harry and *Ned* their pipes soon fill'd
 And rolling clouds of smoke distill'd,
 Then, after each had took a pot,
 Their pipes---and intellects grew hot,---
 Related merry tales and jok'd
 With as much spirit as they smok'd ;---
Ned who was deem'd a sportsman keen
 Told how the *fox* ran o'er the green, III.
 And when they thought him out of danger
 Was catch'd on *Windmill-Hill* by Ranger, IV.
 Where Tom and Joe the whippers-in
 Swore they'd make *parchment* of his skin : V.
 ---Quoth

---Quoth *Harry*, now we have gone before ye,
 Pray *Will* let's hear you tell a story ;---
 But he had no great inclination
 Or talents for confabulation,
 Yet well their manner had perus'd,
 And notic'd all the shifts they us'd,
 A pause did every sentence fit
 To take a whiff and then to spit ;
 Thought he, it seems the true intention
 Of smoking was to help invention,
 Or introduc'd at first, perhaps,
 Only to stop narration gaps,
 And hold depending tale at bay
 While thought dictates what's fit to say,
 Be which it will it is well meant,
 And now to smoke is my intent,---
 Then pipes and 'bacco he fell hard on,
 With " Gentlemen, I beg your pardon
 " For this delay ; but I'll begin
 " As soon as e'er my pipe is in."---
 Yet, when 'twas lighted he said little,
 For long intervals fill'd with spittle,
 And draughts of smoke, and without doubt
 Much more he swallow'd than let out,
 This made him gape for breath much quicker
 Than preaching Methodist---or vicar,
 And almost choak'd with smoke and phlegm
 Began to hiccup, cough and hem !
 Quoth *Harry* (who observ'd the plight
 Poor *Will* was in by's turning white,
 For pipe and face were of a colour),
 Z---ds *Will*, come fill thy pipe up fuller !
 Or must I do it for thee,---shall I ?
 Why man thou art no friend to *Raleigh* ;---
 But *Harry* had no sooner spoke
 But was rewarded for his joke,---
Will long had strove, with griping pain,
 The dose he'd taken to contain,
 With which he now, oh, foul disgrace !
 Saluted *Harry* in the face,
 At the same time, although no fool,
 Mistook his br---ches for *close-stool*,
 Then staggering away to bed,
 Curs'd *Raleigh*, *Harry*, pipes and *Ned*.

Prize.

Ingenious Answers to the Queries, Rebusses, Enigmas, &c. have been received from Mess. John Clarke, William Fininly, Rogers, Joseph James, Caput Mortuum, Miss Greville, Miss Lee, &c. but the prize of ten Diaries fell to the lot of Miss Lee, who is desired to send to Mr. Carnan's, N° 65, St. Paul's Church-yard, for them.---**Such of our Poetical Correspondents as do not find their pieces inserted, we hope will excuse the omission, as the Compiler unfortunately lost the greatest part of their Letters ; but their future favours shall be particularly attended to.

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New QUERIES, REBUSES, &c. to be answered next Year.

I. QUERY, by Cleonicus.

Why is the thick part of the leg called the *calf*?

II. QUERY, by Vulcan.

When a piece of iron is heated red hot and immediately cooled in water, it becomes *blander*, but if left to cool in the open air, *softer*: Can this be accounted for?

III. QUERY, by R. Burrow.

Cotton in his *Virgil Travestie*, pag. 9. has these lines,
Bounce, cries the port-hole, out they fly,
And make the world dance *Barnaby*.

Whence is derived the expression used in the last line?

IV. QUERY, by Mr. Tho. Hatton, *Sen*.

Whether a practical geometer can execute the first problems of geometry *trueſt* with great or small distances?

V. QUERY, by Mr. Dalby.

Whence proceeds the ſaltneſs of the ſea,---and is it more ſo *now* than *formerly*?

I. REBUS, by Miſs Lee.

The top of the *mode* and what never is old,
When join'd, a great genius's name will unfold.

II. REBUS, by Mr. Dalby.

A pronoun connected with half a high place,
Is a pit made for cabbage,---and folks void of grace.

III. REBUS, by Miſs Greville.

A word which ſaves ſome folks from being undone,
And one which means many and ſometimes but one,
When join'd, if you're with it, then you are alone.

IV. REBUS, by Beatrice.

Take half ſuch a number as cannot be few;
The end of an error; and part of a ſcrew;
What's always in priſon, yet never in fear;
What with malt, hops, and water make humming ſtrong beer;
Theſe joined, will tell you what ſome call an evil,
For each day 'tis a hundred times wiſh'd at the devil.

A PARADOXICAL REBUS, by Peter Wilkins.

One thouſand and one; twenty hundred, and fifty,
(You ſee of great numbers I would not be thrifty)
When properly joined, a poet ſublime
Will be form'd, tho' you'll own, no great dealer in rhyme.

An ACROSTIC REBUS, by Mr. Leonard Walker.

A godlike virtue found in ſacred writ;
A Grecian poet fam'd for ſenſe and wit;

A Britiſh

New Enigmas.

21

A British prelate who in exile dy'd ;
 A Roman prince to Livia near ally'd ;
 A place to which (if poets tell us true)
 A fam'd musician went his wife to view ;
 A valiant Greek in heavenly armour cas'd ;
 A false religion through the East embrac'd.
 The initials join'd, a noble port will shew,
 On which old seamen many thanks bestow.

New ENIGMAS to be answered in the next Year's DIARY.

I. ENIGMA, by Mr. J. Keech.

I Am the strangest thing in nature,
 With neither form or make or feature,
 A mere idea, and yet none,
 And am no sooner got than gone.
 The British fair, who much me prize,
 Never beheld me with their eyes,
 (Such eyes as all the world pervade,
 And turn to noon the darkest shade.)
 Possess'd of me, the blooming train,
 Attractive, charm the sighing swain ;
 The melting look, the speaking sigh,
 All doubly please when I am by :
 But, if the nymph my useful aid
 Regards not,---by her heart betray'd,
 She's lost for ever, and her name
 Is handed down to public shame.

Now take me in another view,---
 I'm oft hung up for public shew ;---
 And one hint more.---I'll deign to tell,
 That clowns in *Berkshire* know me well.

II. ENIGMA, by Mr. John Clarke of *Lincoln*.

Ere time began I do my being claim,
 Before bright Sol appear'd I had a name,
 And am the source of every living thing,
 The great original from whence they spring,
 Who, teeming forth out of my fruitful womb,
 By a superior being bade to come :
 No sooner was the powerful *fiat* given,
 Than from my peaceful kingdom I was driven,
 Matter, my deadly foe, usurp'd my throne,
 And spread its power to distant parts unknown,
 Where swift-wing'd atoms lovingly embrace,
 And join together in their destin'd place.
 From me arose the tingy-finger'd morn,
 When first Aurora did the hills adorn,
 The golden ray, the chearing beam of light,
 Whose power dispels the fable shades of night.

The Ladies and Gentlemens Diary.

To journey round the airy globe began,
 And kindly warm the chilly age of man.
 My myst'ries are too dark for vulgar eyes;
 Within my heart the truth in private lies.
 Sometimes, by stealth, when wit and sense are fled,
 I fill the vacuum within the head
 Of one of our great *senatorial* band,
 Who oft 'gainst sense and reason makes a stand;
 Happy he thinks himself of me possess'd,
 And fondly hugs the darling to his breast;
 Whene'er he speaks of me, the list'ning throng
 " Dwell on the melting music of his tongue,
 " The copious accents fall with easy art,
 " Melting they fall and sink into the heart;
 " Wond'ring we hear, and fix'd in deep surprize,
 " Our ears refuse the censure of our eyes."
 To me all vöws and promises do tend,
 And in my faithful bosom ever end.

III. ENIGMA, by Sligo.

From ages past I my existence draw,
 And keep the common robber still in awe.
 Sometimes I'm seen upon the humble ground,
 Sometimes in higher regions I am found:
 Plac'd by the cautious housewife's careful hand
 In midnight watch to take my silent stand.
 There when the wily rambler roams abroad,
 I bar his way and ease him of his load;
 No more with vent'rous step he e'er shall come,
 No more return unto his former home,
 But prostrate laid, shall yield his latest breath,
 And struggling sink into the arms of Death.
 Grimalkin oft complains with out-stretch'd paw,
 When slips the fav'ry morsel from her jaw;
 And fain would make me feel her utmost ire
 Or burn my body in consuming fire.
 No eyes---no legs---no arms---do I possess,
 A mouth I have, but can't a word express.
 But one strong tooth within that mouth is seen
 And they can ne'er escape who come between.
 'Tis said by ancient poets in their Song
 When tuneful harps have charm'd th' attentive thröng,
 That once I sprung from forth a Cambrian's brain
 Who oft had sigh'd and wish'd for me in vain.
 Secur'd their property and did protect
 What locks and bolts and bars could not effect.
 Since when I've been the theme of many a lay
 Sung by brisk virgins on the jocund May:
 Nay, even grave philosophers have taught
 The great advantages with which I'm fraught,

New Enigmas.

23

My use to every housekeeper is known,
And few there are but claim me for their own;
Now I my merit and my worth proclaim:
Consult, ye fair ones, and find out my name.

IV. ENIGMA, by Tycho.

An ancient knight (once fam'd for deeds of arms,
Whose actions fire us, and whose genius warms,
Once in a coward king's reproachful reign
Did fall a victim unto haughty Spain).
Brought me from foreign climes to British land,
Where now in estimation great, I stand.
All ranks of people my acquaintance court,
And to enjoy me eagerly resort,
I favour contemplation's thoughtful brow,
And many a charm on solitude bestow:
Nor less in festive throngs, for there I'm seen,
Where still I sit erect with jocund mien.
The justice grave, who takes his daily fee,
Retires from business to converse with me.
The reverend priest---mattins and vespers o'er,
With me relaxes care, and owns my power.
In Belgia's clime, my company is known,
And every *Mynbeer* claims me for his own;
When the droll jester makes the table roar,
And *Yorick's* thoughts on eagles' pinions soar;
In circling clouds I round the temples twine,
I cheer the drooping heart, and thoughts refine.
Vast funds of treasure into England come,
Which ne'er had been had I remain'd at home.
With wealth I many families supply,
Who for subsistence do on me rely.
But since-contending storms began to roar,
And *feuds unnatural* shook th' *Atlantic shore*;
That wealth decays, *Britannia's* sons do mourn
Their *traffick* lost----but soon may it return.
Heaven grant this pray'r may not be made in vain,
And Peace and Plenty bless great George's reign.

V. ENIGMA, by Mr. Clarke.

In Heaven's wide expanse I had my birth,
Sent down by God, to cheer the mourning earth,
My properties are of Celestial kind
His bounty gave, to bless the human kind.
If grief or wrong, their scorpion stings entwine
I bear with patience nor do e'er repine:
I never vaunt of benefit conferr'd,
Or puff'd with pride, speak an abusive word.
Nor yet in works of wickedness rejoice,
But in the praise of Truth exalt my voice.

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All ill with resignation pure I bear,
 And Faith supports me in my greatest care.
 On Hope's sheet anchor firmly I rely,
 Nor Envy's tooth can e'er my bliss annoy.
 They who confide in me can never fail
 But safely pass thro' life's uncertain vale;
 Happy the man possess'd of me remains,
 No Sorrow hurts him, nor the greatest pains
 Can shake the settled temper of his soul,
 Or draw his thoughts from the Celestial goal.
 But let me add and to the truth attend;
 No selfish mortal can I e'er befriend.
 If pride or spite should rush upon the thought,
 Then my assistance vainly will be sought.
 The good, the honest and religious man,
 Whose upright mind does every virtue scan,
 Whose bosom's not with direful rage possess'd,
 But sweet forgiveness dwells within his breast,
 Who seeks with haste the anxious wretch to cheer,
 And wipes from Sorrow's eyes the falling tear,
 He!---he! alone the rapturous knowledge bears,
 And in his soul my heavenly form he wears,
 That when releas'd from these his earthly chains,
 I'll waft him up to the eternal plains.

VI. ENIGMA, by Mr. J. Bonnycastle.

Ladies, I'm a human creature,
 Flesh and blood as well as you,
 But so mysterious is my nature,
 I am known to very few.
 Just as whim and chance direct
 I or male or female prove,
 Now French politeness much affect,
 And now a haughty Spaniard move.
 Sometimes in starch opinions drest
 Of gravity and deep conceit,
 Anon my humour is express'd
 By quarrelling with all I meet.
 But, tho' I am the oddest wight
 That ever mortal eyes did see,
 Ye lovely fair! your sole delight
 Consists alone in loving me.
 Not Strephon fighting at your feet
 And breathing vows of amorous pain,
 Can half the favours hope to meet
 Which I from you so often gain.
 You too, ye beaux, my charms confess,
 Esteem my worth, and prize me more
 Than misers, when their hoards they bless,
 Esteem and prize the golden ore.

Should

New Enigmas.

25

Should you your chance in Fortune's wheel
Pursue, and gain the lucky fee;
However happy you might feel,
Yet still mankind would wish 'twere me.

If from these hints you find me out,
'Twill pay your trouble ten times o'er,
But after all your search, I doubt,
You'll be no wiser than before.

VII. ENIGMA, by Mr. J. Dalby.

Festina lente, Sirs,—behold!
A hero impudent and bold,
Who dares demand the precedence
Of ladies, lords,---or men of sense;
Should you dispute this, upon trial
You'll seldom find I brook denial;
---Yet am, although such great command,
Obsequious to each turn of hand.

There's no court-spy, with all his arts,
Has my insinuating parts,
Yet at the tables of the great,
And all the cabinets of state,
Know, I mysteriously attend,
But their undoing is my end.
When pride has kindled war's alarms,
And drums and trumpets sound to arms,
Where roaring gun's destructive balls
With dreadful shock salute the walls
Of some strong fort,---if taken, I
Am sure to crown the victory.

Now weary Sol withdraws his light,
And half the world is hid in night,
Ere in the boxes watchmen sleep,
Or city nymphs their vigils keep,
On some dark gloomy hole I fix
To shew circumlocutive tricks;
Just at the front there ready stands
A castle rais'd by skilful hands,
With various windings, intricate
As *maze*, or *labyrinth of Crete*,---
Here a stout chieftain takes his place,
Who only dares to shew his face,
But then, his fortitude is such
When charmed with my magic touch,
With horrid clang darts from the bounds,
While through the dome the noise resounds;
---Strange, although true!---out came this elf
For safety, and to hide himself.

Search all the *pharmaceutic* pack,
From *Dr. Potts* to *Moorfields Quack*,

No

The Ladies and Gentlemens Diary.

No nostrum's found, wherein combine
 The virtues that can equal mine,
 Who am, you'll own, the least inertive,
 The most astringent, and apertive:
 ---Such physic may preserve your life,
 But seldom can a wanton wife,
 In vain, the cure on me depends,---
 I'm counterfeited for her ends.

So Danae fair was thought secur'd
 When within brazen walls immur'd,
 But am'rous Jove with golden charms
 Broke through, and sunk into her arms.

VIII. ENIGMA, by Cleanicus.

Ye riddling wits, to me attend,
 And listen to a common friend,
 For each of you my aid require,
 I turn the verse, and string the lyre.
 Among you oft well pleas'd I'm seen
 If no ill nature steps between,
 But if there should, I quick retire,
 And take the wit, and leave the fire;---
 For there's a set of sober fellows
 Of whom, in truth, I'm always jealous,
 And if I meet with them,---'tis true,
 I'm sometimes beaten black and blue.

And now my pedigree to trace:---
 I'm near as old as human race,
 For the first bride, with *Nix's* assistance,
 Brought *guilt* and me into existence,
 And pass'd me off to her *good-man*,
 As since her *pretty* daughters can.
 With male and female now I'm found,
 This laughing, jesting world around,
 Who play me off on one another,
 On wife, on husband, father, mother,
 And so about from one to t'other.
 By me, 'twas Jacob gain'd the blessing,
 And all the land for his possessing;
 And Judith, by my aid and tricks,
 Sent Holofernes 'cross the styx.
 Uriah found me to his cost,
 To be in battle the first post,
 Where plac'd by me, he lost his life,
 That David might possess his wife.
 Much more I could of ancient lore;
 But I have said enough before:
 And now to come to modern days,
 Where I at balls, park, cards and plays,
 In far more shapes attra& your view
 Than changeful *Proteus* ever knew;

Therefore to trace them were in vain
At *Enfield-Wash*, or in *Cock-Lane*,
Or in the *unknown, Southern main*.

I have a sister, lovely creature!
Who's very like me in her nature,
Who with her poignant wit beguiles
The tedious hours, and wins your smiles;
She is in various colours seen,
But not in either blue or green;
Take one hint more,---if hints you lack,
By all men she's ador'd---when black.

If you a courtier's levee grace,
In hopes to gain a friend or place,
You'll find,---the fates all agree,
Friend, place or pension end in me.

Tho' I am not to place confin'd,
But range among all human kind,
One of my houses may be found
In *Covent-Garden* th' whole year round:
And if you'd know where else I be,
I'm always on the *Change* at three.

IX. ENIGMA, by Calliope.

Far from the busy world's tumultuous noise,
Where anxious care each genial bliss destroys;
Far from the court where adulation reigns,
I seek the peaceful refuge of the plains;
No vaulted roofs conceal my humble head;
By patience nurtur'd, and by virtue fed:
The simple cottager has known me long
The subject of his morn and evening song;
With jocund reed, he tunes his rustic lays,
And echoes me the theme of all his praise;
Fair white-rob'd innocence attends me still,
And smiling peace, secure from every ill.
Long ere the virgin's snowy breast began
To heave and throb, when first she wish'd for man,
Before sly Cupid made her own his sway,
(Whose sovereign power both men and gods obey)
Whether in lonely shades she mus'd along,
Or, in the festive dance, or choral song,
Nimble she tript around about her bed,
Night drew its sable curtains o'er her head,
Upon her steps I ever did attend,
Her sole companion, and her dearest friend.

I soften labour, make the wretched smile,
And cheer the drooping mourner's heavy toil;
And in the gloomy prison oft am seen
Sitting on sorrow's brow with heavenly mien;
The abject slave, who drags his galling chain
Beneath the line in *Africa's* sultry plain,

Deign

The Ladies and Gentlemans Diary.

Deign I, my kindly influence he should share,
 Hush'd all his griefs, and banish'd all his care,
 With fortitude the cumb'rous load he bears,
 And all his mind for future joy prepares ;
 His soul expands with pleasure yet unknown,
 And his hard couch becomes a bed of down.

Judge ye, who can, my name,---from whence I come,
 And be your bosom still my constant home.

X. ENIGMA, *by Mr. J. Bonnycastle.*

When first my origin began,
 Whether before the race of man,
 Or, if I Adam did succeed,
 Philosophers are not agreed :
 But know, ye bards, that I can trace
 From earliest times my noble race,
 And shew that emperors and kings,
 (From whom both life and honour springs)
 Are my progenitors and fires,
 Historians else are arrant liars.
 Moses, the Jewish legislator,
 Than whom, 'tis said, no man was greater,
 When he describes the world's creation,
 You'll find me in the strange relation ;
 And when the seers did prophecy,
 Who in their mouths so much as I ?
 King Solomon, that sapient prince,
 And all his brethren ever since,
 Have us'd me as a common slave
 On all occasions, gay or grave ;
 T'harangue the court, or please the rabble,
 And found no one so serviceable.
 Philosophers of ancient date,
 Held in the world's opinion great,
 Too numerous for me to name,
 To my assistance owe their fame ;
 And modern sages, all agree,
 Are quite as much oblig'd to me.
 See but in these enlighten'd days
 Religion split a thousand ways,
 Each sect for modes of faith contending
 On which Salvation is depending,
 And who to disbelieve's inclin'd
 To hell and Satan is consign'd ;
 In each debate I still preside,
 And all their arguments provide ;
 Still furnish matter for dispute,
 " Confute, change hands, and still confute."
 As o'er a mug of filthy ale
 Sage Philo' tells his baudry tale,
 Or deep in mathematic lore,
 Recounts his various problems o'er,

New Enigmas.

29

The wond'ring audience gaping wide,
Throw both their pipes and ale aside,
And half astonish'd, all agree,
Sage Philo' is inspir'd by me.

To me the learn'd must ever yield,
And logic quit the well-won field,
What I assert you can't deny,
Nor for my wherefore bring a why,
My arguments admit of no reply.
In short, my powerful aid is such,
I never can be priz'd too much;
And those who please to condescend
To use me as their bosom friend,
May safely trust to my alliance,
And bid to all the world defiance.

}

PRIZE ENIGMA (*of 10 Diaries*) by Mr. Leonard Walker.

List, ye fair, a masquerader
Comes his artless tale to tell;
Deem him not a rude invader,
Who can charm the fairest belle.

From the days of grandfire Adam
Down to this auspicious time,
I've delighted ev'ry madam
Who enjoy'd her youthful prime.

Rustic swains, when they are wooing,
Often claim my potent aid;
I, in all their am'rous cooing,
Always please the love-sick maid.

As the best of earth-born creatures
Sometimes widely go astray,
So I've been, by artful features,
Sometimes tempted to betray.

By my zeal to please a fair one,
I old Satan's envy rais'd;
Can this instance be a rare one,
Which the epic bard has prais'd?

No fair nymph did e'er enfold me,
Circl'd in her lilly arms;
Nor did ever nymph behold me,
Whilst I feasted on her charms.

Sweet, O sweet! the thrilling pleasure,
Which to youth I still impart;
Not the miser's darling treasure
Charms so much his anxious heart.

Now, fair maids, I've told my story;
So I humbly bid adieu:
May you still attain fresh glory,
And your swains prove kind and true!

Answers

Answers to the Mathematical Questions proposed in last Year's DIARY.

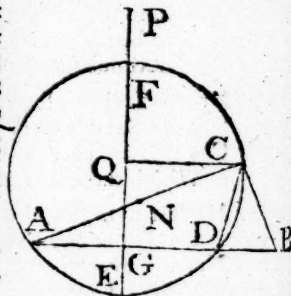
I. QUESTION, answered by Mr. Tho. Hatton.

BY division the equations become $x^2 + y^2 = \frac{a}{xy}$, and $x^4 + y^4 = \frac{b}{xy^2}$,
square the first and we shall have $x^4 + y^4 = \frac{a^2}{xy^2} - 2xy = \frac{b}{xy^2}$, hence
 $2xy = \frac{a^2 - b}{xy^2} \cdot \frac{1}{4} (=n)$ therefore by substitution we shall get $x^2 + 2xy$
 $+ y^2 = \frac{2a^2}{n} + n$, and $x^2 - 2xy + y^2 = \frac{2a^2}{n} - n$, and extracting the
square root, $x + y = \sqrt{\frac{2a^2}{n} + n} \cdot \frac{1}{2}$, and $x - y = \sqrt{\frac{2a^2}{n} - n} \cdot \frac{1}{2} \therefore x = \frac{1}{4}$
 $\sqrt{\frac{2a^2}{n} + n} + \frac{1}{4} \sqrt{\frac{2a^2}{n} - n}$, and $y = \frac{1}{4} \sqrt{\frac{2a^2}{n} + n} - \frac{1}{4} \sqrt{\frac{2a^2}{n} - n}$.

In this manner nearly the solution was given by Mr. Joseph James, of Stoke Bishop, near Bristol, and Mr. Benj. Hayton. Answers were also received from Messrs. Barker, Simmons, Rowley, Moody, Smith, and the proposer.

II. QUESTION, answered by Mr. Jer. Ainsworth.

Construction. Upon AD the given diff. of the segments of the base describe a segment of a circ. AFD to contain the diff. of the angles at the base, draw the diameter EF ⊥ AD. let FE be to GP in the given ratio, and make GQ × GP = the given rectang. Also draw QC = AB, and take CB = CD, and ABC is the triangle required.—For let CB be to CN in the given ratio; then GQ × FE = CB × CA (*Simp. Geom.* 25 3.): GQ × GP :: FE . GP (that is, by construc.) :: CB : CN :: CB × CA : CN : CA; consequently CN × CA = GQ × GP. Also the ang. ABC (CDB) — CAB = ACD. Q. E. D.



Messrs. Keech, Sanderson, &c. observe that the rectang. of the field is given, and thence give very simple constructions.—It was also answered by the proposer, and Mr. Tho. Barker.

III. QUESTION, answered by Mr. Will. Hedley.

In the annexed figure, let $AB = a$, $AD = x$, $DC = y$, and the given property of the curve make $AE : EC :: m : n$; then the sim. triangles,

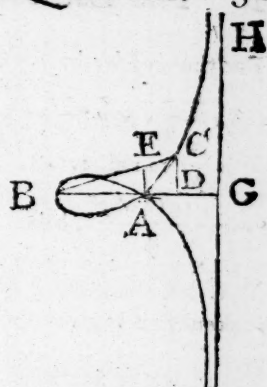
$$+x:y::a:\frac{ay}{a+x}=AE, \text{ and } \sqrt{x^2+y^2}$$

$$\frac{ay}{a+x} = \frac{x}{a+x} \sqrt{y^2+a+x} = EC; \text{ whence}$$

$$\frac{ay}{a+x} : \frac{x}{a+x} \sqrt{y^2+a+x} :: m : n, \text{ hence}$$

$$\text{we get } y = \frac{m \times ax + x^2}{\sqrt{n^2 a^2 - m^2 x^2}}, \text{ for the Equa-}$$

tion of the required curve.



$$\text{The flux. of the Area } y \dot{x} = \frac{ax \dot{x} + a^2 \dot{x}}{\sqrt{\frac{n^2 a^2}{m^2} - x^2}} = \frac{ax \dot{x}}{\sqrt{b^2 - x^2}} + \frac{x^2 \dot{x}}{\sqrt{b^2 - x^2}}$$

$$\left(\text{putting } b^2 = \frac{n^2 a^2}{m^2} \right) \text{ the fluent of which properly corrected is } ab +$$

$$\text{area of quad. whose rad. is } b, = \frac{n}{m} a^2 + \frac{7854 n^2 a^2}{m^2} \text{ for the area of}$$

the whole curve space ACHG.

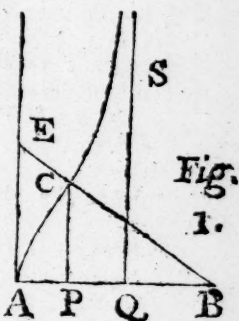
Corol. when $x = \frac{na}{m}$, y is infinite; and consequently GH is an asymptote to the curve:—if $n=m$ the point A will be a *nodus*, or double point of the curve as per Fig.—if n be greater than m , y will be nothing when $x=a$, that is the curve will pass through B,—if n be less than m , then x can never become $=a$, &c. &c.

The same answered by Mr. Jer. Ainsworth.

Let fall the perp. CP and take AQ to AB in the given ratio of C to EA. then by permutation; AQ:EC::AB:EA (that is sim. triang.)::BP:PC. And by reason the ||s EA, PC, EC:AP::BC:BP, therefore *ex aequali* AQ:AP::BC:PC, A Q²:AP²::BC²:(BP²+PC²):PC², and by division A Q²-AP²:AP²::BP²:PC², the nature of the curve required.

Or, making AB=a; AQ=p, AP=x, and PC=y, $-p^2-x^2:x^2::a \propto x^2:y^2 = \frac{x \propto x^2}{p^2-x^2}$, and $y = \frac{ax \propto x^2}{p^2-x^2}$. Hence it

idently follows that if QS be drawn \perp to QP it will be the asymptote of the curve. and moreover if EC be greater than EA the curve will pass through the point B.



For

Answers to Mathematical Questions. 33

$DN = DC \therefore AD - CD (DN) = NA$. Now the Locus of the centers ($S, C, m, \&c.$) of an infinite number of circles passing through the point B and touching the circ. A , is an hyperbola whose cent. is M , vertex S , and asymptote Mb ; and since $CN \parallel mS$, and MCn bisects $S m$, it follows that CN is a tang. to the hyperb. in the point C ; consequently a line drawn from any other point of the hyperb. $\parallel mS$ will meet AB on that side of N next B , $\therefore NA = AD - DC$, is a minimum.

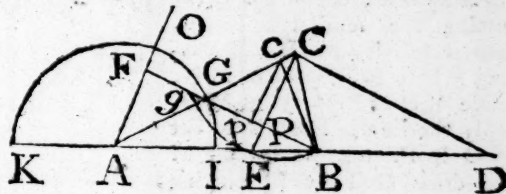
Because QS , is \perp to a line bisecting the $\angle KBA$, and $CN \parallel QS$, CR and QS are $\perp BP \therefore BP$ bisects the $\angle KDA$; — hence the construc. becomes much more simple, thus, — having drawn Bb to bisect the $\angle KBA$, through P draw AC so that $PC = CB$, and C is the vertex of the Δ .

Here it is to be observed that AP must always be less than AB ; but greater than AB ; or which is the same thing, the $\angle BOM$ made by the asymptote and Bb must always be greater than a right one, otherwise a tang. cannot be drawn to the hyperb. $\perp Bb$, and in that case the point N will fall in A , and the *min.* becomes $= 0$; — hence it follows that AD must always be greater than AC . If instead of a *min.* $AD - AC$ was to be a given quant. as AS , draw $Sm \parallel AK$, then find the center m , as before, and it will be the vertex of the Δ .

The same answered by Mr. George Sanderfon.

Construc. About A as a center, and with the given difference of the sides as radius describe the semicircle IGK , draw AO making the $\angle BAO$ equal to half the supplement of the given one, draw BF

$\perp AO$ cutting the semicirc. in G , bisect GB in P , and through G draw AC to meet PC drawn \parallel to AO in C ; join CB , and draw CD meeting $(AB \text{ produced})$ in the given angle in D , produce CP to meet AB in E ; and AE is the *min.* required.



Demonst. Since CE is $\parallel OA$ the $\angle DEC = DAO =$ to half the supplement of CDE the given \angle by construction, the angles DEC, DCE are equal and $CD = DE$, also $AD - CD = AE$; now as GB is bisected by the $\perp PC$, and the points A, G, C in a right line, a circle with CG radius touches the semicircle and will pass through B (Simp. Geom. b. iii. prob. 2 and 7) therefore $AC - CG = AG (= AI)$ the given difference; but because the triangles EBP, ABF are sim. and all the angles constant, and the triangle GCB isosceles, and the $\angle BGC$ in the circumf. of the semicirc. IGK , the vertex C (or the center of a circle whose circumf. touches the semicircle) must always be found in a line \parallel to AO , therefore when their distance FP is a minimum, AE must be a minimum; take Fp less than FP , and make $pc \parallel AO$, with Bc radius describe the arc of a circle to cut BF (produced if necessary) in g , then $pg = Bp$ (Simp. Geom. b. iii. p. 2.) $= GP + Pp$, whence it is manifest the circle

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circle with B c radius cuts or includes the semicircle $I G K$, therefore no circle can be found whose center is in a line \parallel to $A O$, and dist. less than $F P$ to touch the semicircle $I G K$, therefore $A E$ is a minimum.

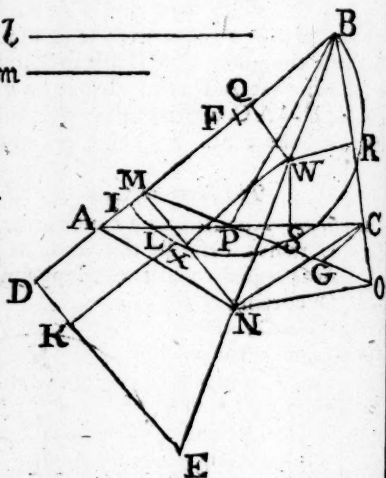
When the $\angle B A O$ is such that $B F$ neither cuts nor touches the semicircle, $C D$ may be constructed equal to $A D$, or their diff. $A E$ will be nothing.---In the other part of the data where $C D$ is to be greater than $A D$ it must be for a given quantity, as their diff. will be nothing when a minimum.

Mr. Jer. Ainsworth constructed this prob.

V. QUESTION, answered by Mr. Joseph Keech.

This question may be reduced to that of having the perimeter, the vertical angle, and the line bisecting the base, of a triangle, given.

Const. Make $B D = \frac{1}{2}$ the perimeter, make the angle $D B C = \angle$ given angle, which bisect with the line $B E$ meeting a perpendicular from D in E , take $B F$ a third part. to $B D$ and $D E$, and with F center and $F B$ radius describe a semicircle $B L I$, take $D K =$ to the side of a square which is the difference of the squares of $D E$ and l , the bisecting line; draw $K L \parallel B D$ cutting the semicircle in L , thro' $L \parallel D E$ draw $M L N$ cutting $B D$ in M , and $B E$ in N , make $B Q = B M$, join $M O$, apply the line l from B to cut $M O$ in P , take $P G = P M$ and draw $G C \parallel B M$ cutting



$B O$ in C , draw $C P A$, and $A B C$ will be the triangle required.

Dem. Draw $N A, N C, N O$, and take $N W = N A$, and let fall the \perp s $W Q, W R, W S$ from W on the sides of the triangle, draw $W X \parallel B M$ cutting $M N$ in X , and let $m \times B D = A S C$; it is evident by const. that $A B C =$ vertical angle, $B P = l$, and that $A C$ is bisected in P ; but since the angles $B C N$ and $B A N$ are equal to 180° . a circle will pass thro' the points A, B, C, N and therefore by Simson's Trig. prob. 11, and oracle quest. 67, $B M = \frac{1}{2}$ the sum of the sides, $A M (= C O = P S) =$ half their difference, and W the center of the inscribed circle and $\therefore W X = A P = Q M \therefore B Q =$ excess of the base above half the perimeter of the $\Delta A B C$; but by Simson's Geo. 11. III: $B M^2 - B P^2 = A P^2 - A M^2 = A S C$ (by 9. II of same) and by const. $B M^2 - B P^2 = 2 B M - D B \times B F$, and $2 B M - D B = B Q$ (if $B D = \frac{1}{2}$ perimeter of the $\Delta A B C$) \therefore by equality $F B Q = A S C = B D \times m \therefore F B : B D :: m : B Q$ and $D E^2 (= D B F) : B D^2 :: A S C (= B D \times m) : D B Q$ which is prop. v. Simson's Trig. and therefore $B D =$ half the perimeter of the $\Delta A B C$.

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The same answered by Mr. Jer. Ainsworth.

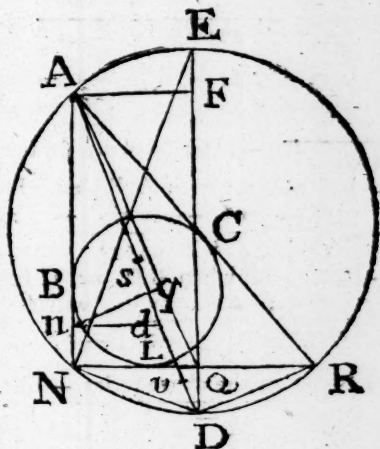
Analysis. Imagine the triangle ANR to be circumscribed by the circle $NAER$ whose diam. DQE is \perp to NR . Let fall the \perp AF , and draw EN , ND , DR and AD ; also, from q , the center of the circle to which AC and AB are tangents, raise $qn \perp$ to Aq , and nd to An , and make $qs = qd$.---Then since $AD^2 (= DF \times DE) : DF \times 2DQ :: DE : 2DQ$, by conversion $AD^2 : AD^2 - 2DF \times DQ :: DE : DE - 2DQ$; but it is well known that $qD = ND$, and by Euc. 4. 2. that $Aq^2 + qD^2 + 2Aq \times qD = AD^2$, therefore $Aq^2 + ND^2 + 2Aq \times ND : AD^2 - 2DF \times DQ :: DE : DE - 2DQ$, that is by sim. figures $Ad : Ad - 2dq = As$. And $Ad \times Ad^2 - 2DF \times DQ = As \times Aq^2 + ND^2 + 2Aq \times ND$, but $ND^2 (DE \times DQ) : DQ^2 :: DE : DQ$ that is $Ad : dq$, or $Ad \times DQ^2 = dq \times ND^2$, which being added to what was before found gives $Ad \times AD^2 - 2DF \times DQ + DQ^2$, or by Euc. 13. 2. $Ad \times AQ^2 = As \times Aq^2 + 2Aq \times ND + Aq \times ND^2$, wherefore $\frac{Ad}{Aq} \times AQ^2 - As \times Aq = ND^2 + 2As \times ND$;---hence this

Construction. Constitute the rectangle under Av and Aq equal to $\frac{Ad}{Aq} \times AQ^2 - sAq$, and take qD , DN each equal to the lefs of two reciprocals to Av , Aq , and which differ by $2As$, and from N draw the tangent NQR which will be that required.

Limitation. If AD cross the circle in L , AQ must not be less than AL .

We have been favoured with a more elegant solution to this question from the same; and we are very sorry it came too late to be inserted in the room of the above.

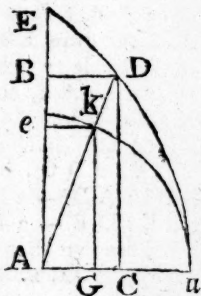
A different construc. was also given by the proposer, which were all the answers we received to this difficult prob.



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VI. QUESTION, answered by Mr. Tho. Todd.

If $p = 3.14159265$, &c. $z = BA = \text{arc } k u$ by the quadratrix; $y = BD = AC$; and $r = Au = 20$ inches half the bung diameter; then by the circle, $kG = eA =$



$$z - \frac{z^3}{6r^2} + \frac{z^5}{120r^4} - \frac{z^7}{5040r^6} + \text{&c. } e k$$

$$= AG = r - \frac{z^2}{2r} + \frac{z^4}{24r^3} - \frac{z^6}{720r^5} +$$

$\frac{z^8}{40920r^7} - \text{&c.}$ and by similar triangles $Gk = eA : ek :: AB(z) : BD = y =$

$$r - \frac{z^2}{3r} - \frac{z^4}{45r^3} - \frac{z^6}{945r^5} - \frac{z^8}{4725r^7} - \frac{z^{10}}{93555r^9} - \frac{z^{12}}{638512875r^{11}} - \text{&c.}$$

and when BD , or y , becomes the semi-head diameter = 15 inches; AB , or z , will be half the length of the cask = $r \sqrt{.713570176252}$, &c. $= r \times .8447308 = 16.894617$ inches found

by reverting the above series. — Therefore $\dot{S} = p \times \overline{BD}^2 \times \overline{BA} =$

$$p \dot{z} \times r - \frac{z^2}{3r} - \frac{z^4}{45r^3} - \frac{z^6}{945r^5} - \text{&c.} \dot{z}^2 = p \dot{z} \times r^2 - \frac{2z^2}{3} +$$

$$\frac{z^4}{15r^2} + \frac{2z^6}{189r^4} + \frac{z^8}{675r^6} + \frac{2z^{10}}{10395r^8} + \text{&c.}$$

the fluxion of the solid generated by the revolution of the space $ABDU$ about BA ,

whose fluent $S = p \times r^2 z - \frac{2z^3}{9} + \frac{z^5}{75r^2} + \frac{2z^7}{1323r^4} + \frac{z^9}{6075r^6}$

$$+ \frac{2z^{11}}{114345r^8} + \text{&c.}$$

the solid itself; which, when $z = r \sqrt{.713570176252}$

gives $S = 21230.40058 \times 1 - \frac{2}{9} \times .71357017 + \frac{1}{75} \times .71357017^{1.5}$

$$+ \frac{2}{1323} \times (.71357017)^3 + \frac{1}{6075} \times .71357017^4 + \frac{2}{114345} \times .71357017^{1.5} + \text{&c.}$$

$= 21230.40058 \times .84881312 = 18020.64255$, &c. cubic-inches: Twice which, is 36041.285 ditto = 127.8099 ale gallons, the contents of the cask required. Hence we may also find the area A .

For $\dot{A} = BD \times \dot{z} = r \dot{z} - \frac{2z^2}{3r} - \frac{z^4}{45r^3} - \frac{2z^6}{945r^5} - \frac{z^8}{4725r^7} - \frac{2z^{10}}{93555r^9} - \text{&c.}$

$$\therefore A = r z - \frac{z^3}{9r} - \frac{z^5}{225r^3} - \frac{z^7}{6615r^5} - \frac{z^9}{1029105r^7} - \text{&c.}$$

= area of $ABDU$, the same (all but the last two terms) as given by Dr. Wallis in his Algebra, p. 344

The proposer, Mr. William Wilkin, intended to have given a solution

Answers to Mathematical Questions. 37

tion, but death untimely prevented him; we mention with the utmost concern the loss of this very ingenious young gentleman, who, to a most engaging and amiable disposition, united those talents which bid fair to have rendered him one of the greatest mathematicians of the age. He died on Jan. 15, 1777, in the 24th year of his age.

VII. QUESTION, answered by Aumuncim.

The series $\frac{2 \cdot 4 \cdot 6}{3} + \frac{4 \cdot 6 \cdot 8}{3 \cdot 3} + \frac{6 \cdot 8 \cdot 10}{3 \cdot 3 \cdot 3} + \&c.$ is $= 8 \times :$
 $\frac{1 \cdot 2 \cdot 3}{3} + \frac{2 \cdot 3 \cdot 4}{3 \cdot 3} + \frac{3 \cdot 4 \cdot 5}{3 \cdot 3 \cdot 3} + \&c.$ hence putting $n =$ the num-
 ber of terms required, and $s =$ their sum, we get, by the method of
 $8nnn$
 increments, $s = \frac{12}{3^n}$, and the next succeeding term, or $s =$

$$\frac{8nnn}{3^{n+1}} = \frac{8vvv}{3^v}, \text{ putting } v = n, \text{ hence, by examp. 14. prop. 13.}$$

$$\text{Emerson's Increments, the integral is found} = - \frac{4vvv + 6vv + 6v + 3}{12 \cdot 12 \cdot 2} \cdot \frac{3^{v-1}}{3^{v-1}} \\ = -81, \text{ when } s = 0, n = 0, \text{ and } v = 1, \text{ hence the correct integral} \\ \frac{4vvv + 6vv + 6v + 3}{12 \cdot 12 \cdot 2} = \frac{6}{3^{n+1}} \times : \frac{2 \cdot 5 \cdot 3}{2} \cdot \frac{7}{2}$$

Corol. when n is infinite the sum is $= 81$.

In this manner nearly the answer was given by Mr. J. Ainsworth.

Mr. Benj. Hayfon, without the method of increments, very readily

$$\text{finds the sum} = 81 \times : 1 - \frac{n+2}{2} \cdot \frac{n+3}{3^{n+1}} - n \cdot \frac{n+1}{2} \cdot \frac{n+3}{3^{n+2}} \\ + n \cdot \frac{n+1}{2} \cdot \frac{n+2}{3^{n+4}}, \text{ where } n \text{ represents the number of terms re-}$$

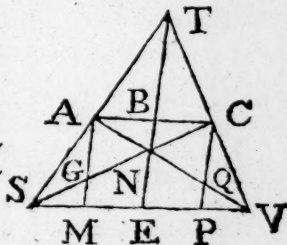
quired.

This question was also answered by Mr. Todd, and the proposer.

VIII. QUESTION, answered by Messrs. J. Merritt, J. Ainsworth, T. Moss, (the proposer) and J. Hampshire; all their demonstrations being the same.

Let TN be produced to E , and draw $CP, AM \parallel$ thereto. Then by reason of the parallels and sim. Δ s, we have $AM : AG :: ET : TN :: CP : CQ$, and alternately $AM : CP :: AG : CQ$ (that is, because the Δ s AGN, CNQ are sim.) $:: AN : NQ :: AB : BC$, by sim. Δ s. $\therefore AM : CP :: AB : CP$.

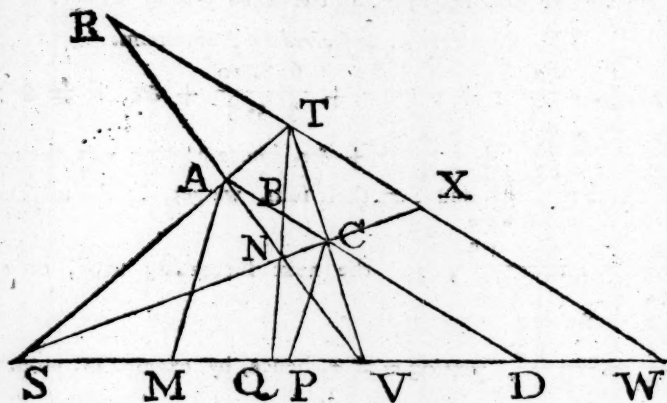
Q. E. D. The demonstration is not materially different if the point N be taken without the triangle.



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The same answered by Mr. J. Burrow.

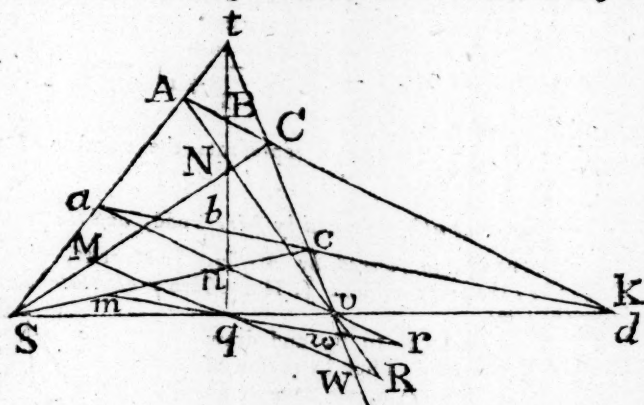
Draw RTW through the vertex T of the triangle cutting the base SV in W , and SC in X ; then by sim. triangles, $RT : TW :: AC$



$: CD$, and $TW : TX :: AD : AC$, therefore $RT : TX :: AD : DC$; but $RT : TX :: AB : BC$, therefore $AB : BC :: AD : DC$; again $AD : DC :: AM : CP$, therefore $AB : BC :: AM : CP$. $Q. E. D.$

Let the lines be drawn as *per figure*, then from above we have $ab : bc :: ad : dc$, and $ab : bc :: rq : qm$, also $ad : dc :: rq : qw$ and $rq : qm :: rq : qw$, therefore $qm = qw$. Again $qw : dc :: qv : vd$, and $qm : dc :: qS : Sd$, also $qv : vd :: qS : Sd$, therefore $Sq : qv :: Sd : dv$.—Hence it will appear that if any two lines SC , SA be drawn intersecting in the line tn in N and cutting the

sides in A and C , then if AC be drawn cutting Sw produced it will cut it in the point d where ac cut it before; for let it cut it in k ,



then by the last, $AB : BC :: Ak : kC$, and drawing $WqM \parallel to AC$ Wq may be proved equal to qM as before; and $qW : Ck :: qv : vk$, also $qM : Ck :: qS : Sk$, therefore $qv : vk :: qS : Sk$, but we have proved before that $qv : vd :: qS : Sd$, wherefore $vk : kS :: vd : dS$, and by division $vk : vS :: dv : vS$, consequently $vk = vd$. Corol.

Corol. 1. If tS , $t v$ be two lines given in position, and d any given point, and if any lines dS , da , dA , &c. be drawn from d cutting the lines tS , $t v$ in the points a , A , c , C , &c. and if the points $S c$, va , SC , vA be joined then the locus of all their points of intersection n , N , &c. will be a right line.

Corol. 2. If tS , tq , $t v$ be three lines, and d a point taken so that $Sd : dv :: Sq : qv$, then if any line whatever dA be drawn cutting the lines aforesaid, AB will be to BC as Ad to dC , &c.

Corol. 3. Hence if Sv be any line, q and d points taken in it, so that $Sd : dv :: Sq : qv$, and vt be any line given in position, then if any lines dc , dC be drawn from d cutting vt in c , C , and if Sc , SC , be joined, and qm , qM drawn \parallel to dc , dC , cutting Sc , SC in m and M , then will the locus of all the points m , M , be a right line \parallel to vt , and q will be a point equally distant from vt and mM .

Demonstrations were received from Messrs. Keech and Sanderfon.

IX. QUESTION, answered by Mr. Todd (the proposer).

If $x =$ years, from the equated time to the last term, $b = 6$ years the time between the first and last debt D , $p = 1000$ l . $r = .05$, and

$n = 20$ l . then per Malcolm, $\overline{b-x} \times pr = \frac{Drx}{1+rx}$ (from which $x =$

$\frac{\frac{b}{r} + \frac{m^2}{4}}{\frac{1}{2}} - \frac{m}{2}$ where $m = \frac{D}{pr} + \frac{1}{r} - b$) and $\overline{D+p} \times rx =$

$n + pbr$ by the Quest. hence $D = \frac{n + pbr}{rx} - p = \frac{bpr - prx}{bpr - prx}$

$\times \frac{1+rx}{rx}$ from above, solved $x = \frac{b}{2} + \frac{b^2}{4} - \frac{n}{pr^2} \Bigg| \frac{1}{2} = 4$, 'and

2 years, and thence $D = 600$, and 2200 l . Hence this quest. admits of two answers, for when $x = 4$ years, $D = 600$ l . and when $x = 2$ years, $D = 2200$ l .

Scholium. The reason of Malcolm's equality of interest and discount at his equated time is shewn thus. If $p =$ debts past, due at any time after the first debt comes due, $r =$ their interest at that time, $D =$ debts then not due, and $d =$ their discount; then at that time the money due to the creditor $= p + r + D - d$, and when $r = d$, then $p + D =$ debt due to the creditor; for at that time the interest and discount become equal and contrary, destroy, or vanish out of the question, which can only happen at Malcolm's equated time.

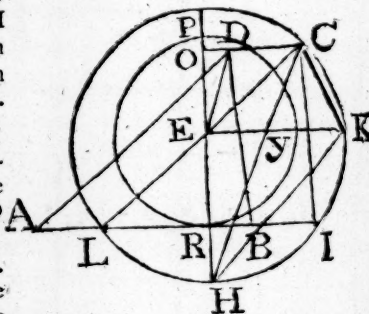
Perhaps it may not be improper to remark that Malcolm's double sign \pm put in his theorem for the equated time, is not right, because it may be proved that in every case the negative sign will obtain. Also, his direction for finding the equated time when there are more debts than two is also false on his own hypothesis, as may be easily proved by trial. Is it not therefore surprizing that most of our arithmetical writers since his time, should so exactly copy these errors into their books as known truths? It is the old method only (long in use before Sir S. Morland's time) that gives the same advantage to the creditor in the whole time, as by the equated time, allowing simple interest;

interest; whereas Malcolm's method always gives more money to the creditor, as is shown above, than could be made by receiving the debts as they become due.

Mr. Dalby gives a solution as follows: Put $a = 1000$, $r = .05$, the rate of interest; $n = 6$ years, and $x =$ the equated time after the first payment is due; then will arx be the interest of a for x time; now to gain any advantage by receiving these payments according to Malcolm's rule, (let D be what it will) this interest must be made use of as a principal; and its interest for $n - x$ time in the present case $= 20l.$ that is $ar^2nx - ar^2x^2 = 20$, in numbers $15x - 2\frac{1}{2}x^2 = 20$; hence $x = 2$, and 4 , for the equated times; and the sums whose discounts for the remaining 4 and 2 years, are equal to the interests of a for those times are $600l.$ and $2200l.$ for the values of D .

X. QUESTION, answered by Mr. John Hampshire.

Construc. Let R P be the given circ. E its cent. \perp to the diam. R P take R I, R L each $= \frac{1}{2}$ the given segm. of the tang. and on L I describe a circ. to contain the given \angle , draw E K \parallel R I, and join K H, then by Simpson's Geom. 5.



18. take HC so that $HY + N \times HY = HK^2$ (N being the bisecting line, or dist. of E from the given \angle) draw CL, CI; also $CO \parallel EK, ED \parallel CY, DA, DB \parallel CL, CI$; and the thing is done. For join CK, then because the $\angle EKH = \angle HKC$, and the $\angle CHK$ common, the Δs CHK, KHY are sim. and so $HC : HK :: HK : HY$, but $HY + N : HK :: HK : HY$ (by const.) hence by equality, $HC = HY + N$, $\therefore CY = N$; and by const. the $\angle LCI$ = the given \angle , and the Δs LCI, ADB sim. and equal $\therefore DE = CY = N$, and $AB = 2 LR$.

The same answered by Mr. George Sanderson.

Construc. On AB the given segment of the tang. describe the segment of a circ. to contain the given \angle , draw the diam. $GH \perp AB$, and take $GO =$ the dist. of the cent. of the given circle and \angle made by the lines given in position, about the cent. o describe the given circ. take $DP = Oe$ the rad. and draw $PI \parallel AB$; from H draw HC cutting PI in F and AB in E such that $FC = GO$, then draw the rad. $Oe \parallel CH$, and lastly draw the tang. bea to meet or cut GA and GB (produced if necessary) in a and b , and GH in t , and the thing is done.

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A geometric diagram showing a circle with center P. Points A, B, C, D, E, F, G, H, I, K, M, N, O, Q, R, S, T are labeled. Lines connect these points to form a complex polygonal shape. The diagram is used to illustrate a geometric proof or construction.

Demonstrations

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$PBE = 2 \triangle PID$. Now, by construction the $\triangle PIC =$ trapez. $AIPB$; wherefore, by adding the $\triangle PID$, twice the $\triangle PID$ with the $\triangle PCD$, that is, the $\triangle s PCD$ and PBE , will be equal to the trapez. $ADPB$.

The same answered by Mr. G. Sanderfon. See the preceding figure.

Const. Draw $PH, PQ \parallel AB, AC$ respectively, then if the $\triangle HCP \sqcap$ trapez. $AHPB$, make $\triangle BPK =$ the diff. then produce QK till $QE \times KE = 2HP^2$ ($2AQ^2$) lastly, from E draw EPD and the thing is done. For letting fall the $\perp PG$; the $\triangle s QPE, HDP$ are sim $\therefore QE^2 : 2HP^2 :: \triangle QPE : 2HDP$ (*Simp. Geom.* 26. 4.) that is $QE^2 : QE \times KE :: QE \times PG : 2HDP :: QE : KE :: QE \times PG : KE \times PG \therefore KE \times PG$ ($\triangle KPE$) $= 2HDP$; but $\triangle HDP + DPC$ ($\triangle HPC$) $+ BPK =$ trapez. $APBH$, (construc.) add to both $\triangle HDP$, then $2HDP + DPC + BPK = AHPB + HDP (=ADPB)$ but $2HDP$ has been proved to be $=PKE$, $\therefore KPE + BPK (=BPE) + DPC = ADPB$ as required.

When $\triangle HCP \sqcap$ trapez. $AHPB$, the diff. must be set off on the other side of B .

The same answered by Mr. Jer. Ainsworth.

Analysis. Draw $PF, PF \perp$ and $PM, PQ \parallel$ to AC and AB ; and bisect AC in G : also make $BK = BA$ and draw PA . Then by the nature of the question the $\triangle s PEB = PAB = PDA - PDC$, consequently $2PF \times DG = PH \times KE$, or $2PF : PH :: KE : DG$, in which ratio therefore take LE to AD , then $2PF : PH :: LE : AD$, hence this *const.* Take $Lv = 2AM$, and make $ME \times Ev = AM \times Lv$, and EPD will be the line required. For since $ME \times Ev = AM \times Lv$, or $Ev : Lv :: AM : ME$, by composition $LE : Lv :: AE : ME$ (that is, by reason of the $\parallel s$) $:: AD : PM$, and alternately $LE : AD :: Lv : PM$; but $2PF \times PM =$ twice the parallelogram $PM AQ = 2AM \times PH = Lv$ ($2AM$) $\times PH$, or $Lv : PM :: 2PF : PH$; therefore $2PF : PH :: LE : AD$.

A construc. to this Quest. was given by Mr. Keech; and an algebraic solut. by Mr. Woolcott.

*** We have received many ingenious answers to the Prize Question, but as several of our Correspondents are of opinion that it admits of a Geometrical solution, we shall, at their request, defer giving any till another Year.

ARTICLE XIV.

A Specimen of a Method of finding Rules for the Extraction of Roots. By Reuben Burrow.

LET N be the number whose root is required, $a + x$ its root and a^n the nearest power to N , and let A and B be indeterminate coefficients.

Assume

Assume $a : a + x :: A a^n + B N : \frac{a+x \times A a^n + B N}{a} =$

$$\frac{a+x \times A a^n + B \times a+x}{a} = \frac{a+x \times A a^n + B \times a+x}{a}^{n+1}$$

$$= (A+B) a^n + (n+1 \times B + A) a^{n-1} x + \frac{n+1 \cdot n}{2} B a^{n-2} x^2$$

$$+ \frac{n+1 \cdot n \cdot n-1}{2 \cdot 3} B a^{n-3} x^3 + \&c. \text{ Then let such values be as-}$$

sumed for A and B as may make this last expression consist of parts or multiples of the given quantities a^n and N, or nearly so, and then the first, third and last terms of this proportion being given; the second will be found by proportion, nearly.

Example. Let $n=2$, $A=3$, $B=1$, then $\frac{a+x \times A a^n + B N}{a}$

$$= 4 a^2 + 6 a x + 3 x^2 + \frac{x^3}{a} = a^2 + 3 a^2 + 6 a x + 3 x^2 \text{ nearly,}$$

or $a^2 + 3 (a^2 + 2 a x + x^2) = a^2 + 3 N$; Wherefore $3 a^2 + N$
 $= 3 N + a^2 :: a : a + x$. Hence the following rule for extracting the
 Square Root. Find the nearest square to the given number whose root is
 required, then thrice the nearest square, added to the given number, is to
 thrice the given number added to the nearest square, as the root of the
 nearest square, to the root required, nearly.

Ex. Let the square root of 2 be extracted; Here $N=2$, assume
 $a=1$, $\frac{a^2}{2}$ then $a^2=2$, $25 \cdot 8, 75 : 2, 25 :: 1, 5 : 1, 4142$; then re-
 peating the operation $a=1, 4142$ and $a^2=1, 99996164 \cdot 7, 99988492$
 $7, 99996164 :: 1, 4142 : 1, 4142135623730947$ which is true to 16
 places, and only errs 2 in the last figure, which should be a 9.

In order to get a rule for extracting the cube root, let $n=3$, $A=2$
 and $B=1$, then $\frac{a+x \times A a^n + B N}{a} = 3 a^3 + 6 a^2 x + 6 a x^2$

$$+ 4 x^3 + \frac{x^4}{a} = a^3 + 2 (a^3 + 3 a^2 x + 3 a x^2 + 2 x^3) = a^3 + 2 N$$

nearly, by rejecting x^3 and $\frac{x^4}{a}$ which are very small. Hence the fol-

lowing rule for extracting the Cube Root.
 Find the nearest cube, to the given number whose root is required; then
 twice the nearest cube, added to the given number, will be to twice the given
 number added to the nearest cube, as the root of the nearest cube, to the root
 required; then if this last quotient be assumed as the root of the nearest
 cube and the operation repeated, the root may be found to any exact-
 ness requisite.

Cor. 1. Another approximation for the cube root may be had by
 substituting 5 for A and 1 for B, but not so exact as the above.

Cor. 2. Because $3 a^2 + N : 3 N + a^2 :: a + \frac{1}{3} N : N + \frac{1}{3} a$
 therefore

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therefore $a + \frac{1}{3} N : N + \frac{1}{3} a :: a : a + x$ and this rule is the most convenient for extracting the square root when the given number will divide by 3; and the same for others.

Cor. 3. Also because $2 a^3 + N : 2 N + a^3 :: a^3 + \frac{1}{2} N : N + \frac{1}{2} a^3$ therefore $a^3 + \frac{1}{2} N : N + \frac{1}{2} a^3 :: a : a + x$ which brings out the cube root in fewer figures when the given number is divisible by 2. &c.

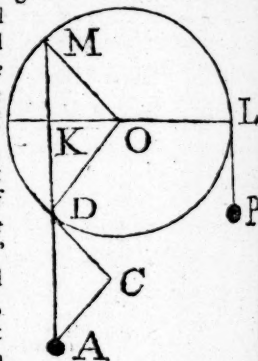
A R T I C L E XV.

Remarks on some Criticisms concerning the Property of the Lever, &c. by Reuben Burrow.

HAPPENING lately to meet with a volume of Philosophical Essays, published in 1766, by that excellent Geometrician Dr. Hamilton, Professor of Philosophy at Dublin, wherein are several objections made against Sir Isaac Newton's proof of the property of the Lever, I made enquiry whether these objections had ever been refuted? and being answered in the negative, I have taken the liberty of pointing out where I apprehend the Doctor is mistaken.

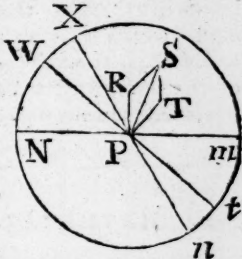
In the second corollary to the third law, Newton assumes two principles as self-evident; one of which is, that equal and contrary forces acting perpendicular to any two radii of a wheel at equal distances, will prevent it from turning about its center; the other is, that any weight A suspended by a cord fastened at D will have the same force in the direction DA as it would have if fastened at any other point in that line. The first of these is very evident, and the last remarkably so; for as the weight A is here the only force that acts in the direction DA, and as that remains the same whether the cord be fastened at D or at K consequently the force in the direction DA is not in the least varied, whatever part of the line DM may be assumed for the point of suspension.

—This is all that Newton supposes; but Dr. Hamilton seems to understand it, as if Newton had assumed for a principle “that the force to turn the wheel about its axis,” was the same whether the cord was fastened at D or at K; that it is so there is no doubt, but that only follows as a corollary and is not at all pre-supposed in the demonstration which proceeds totally independent of that consideration, and requires only this self-evident assumption, “that the force in the direction DA is the same, whether the string be fastened at D, K or M.” Thus let there be given the weight LP acting perpendicular to LO at L, and the force be required which acting \perp to OK at K will balance it. Now by the first assumption if $OD = OL$ it must be a force $DO \equiv LP$ which acting perpendicular to DO will balance LP; but



the force required is to act in the direction DA , by corollary 1, KDA must be perpendicular to KL , and CA to CD , in order to find the force DA , which, acting in the direction DA , will be equivalent to DC in the direction DC , now $DC : DA :: OK : OD$, therefore $LP : DA :: OK : OL$ and therefore the lengths of the arms are reciprocally as the weights.

It may not be amiss to annex here a few easy corollaries to the 1st and 3d laws of motion. Let $NXmnP$ be a globe, $NXmn$ a section, through its center, and P a point where the diameter, perpendicular to the plane $NXmn$, meets the surface; and let PT , perpendicular to this diameter, represent the globe's velocity about the axis Xn and PR in the same plane with PT , represent the velocity about the axis Nm ; then the globe will revolve about a new axis in the same plane with Xn and Nm : for the line PS which represents the velocity compounded of PT and PR , or the velocity with



which the globe revolves about the new axis, lies in the same plane with RP and PT ; but the axis of revolution lies in a plane passing through the center parallel to this plane, and its direction is perpendicular to that of the tangent PS : Hence, $NPR = XPT = WPS$ wherefore $RPT = NPX$, $SPT = WPX$, and $NPW = RPS$; let $V = PT = RS$, $v = PR = ST$; then $PR : PT (RS) :: s. PSR : s. RPS$; that is $v : V :: s. WPX : s. NPW$; wherefore the velocity about the axis Nm is to the velocity about the axis Xn , reciprocally as the sines of the angles NPW and WPX made with the new axis Wt . Again, $PR : PS :: s. PSR : s. PPS = s. RPT = s. NPX$, that is, $PR : PS :: s. XPW : s. XPN$; also $PT : PS :: s. NPW : s. XPX$. Hence if x be put to represent the velocity PS , $V : v : x :: s. NPW : s. WPX : s. XPN :: PT : PR : PS$.

The above is not restricted to globular bodies only, but is equally applicable to planes and solids of different kinds, and may be of use in several branches of philosophy, particularly in determining the procession of the equinox, &c. and what is done above for two forces may be applied to any number in the same manner as is usually done in composition and resolution of forces on the same or different planes.

ARTICLE XVI.

An easy method of determining experimentally the Curve which a shell describes in its flight. By Reuben Burrow.

THOUGH the method of determining the curve which a military shell actually describes be difficult from theory, yet it is so easy in practice that I should scarcely have thought the following worth insertion, had not Captain Williams of the Royal Artillery publicly proposed

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posed the thing as a question of some importance, and afterwards solved himself by a way which cannot be true in theory and must be of insuperable difficulty in practice.—The method I would propose, is by means of an instrument for drawing perspective views (which was invented by Sir Christopher Wren and published in the Philosophical Transactions; and afterwards re-invented and improved by Gilbert Warr) namely by placing this instrument parallel to the range of the mortar, and when “live shells” are fired, to keep that point of the instrument intended to trace outlines continually between the eye and the shell (which may easily be done as shells do not move quick and are easily seen) then the pencil will describe a curve exactly similar to that of the shell, for the same reason that the sections of a cone cut parallel to its base are similar.

New MATHEMATICAL QUESTIONS to be answered in next Year's DIARY.

[1] XXVI. QUESTION, by Mr. Tho. Hatton.

GIVEN $x^2 + xy + y^2 = a$
 $x^4 + x^2 y^2 + y^4 = b$ } required x and y .

N. B. This Quest. was proposed in Martin's Mag. but admits of a neater solution than is there given.

[2] XXVII. QUESTION, by Amuneim.

TO find two numbers such that the sum or diff. of their squares lessened by unity shall in each case be a rational square.

[3] XXVIII. QUESTION, by Mr. Will. Hardy.

LET there be two right angled triangles BDA, CQA whose hypotenuses AB, AC are given and meet in the point A making a given $\angle BAC$; tis required to determine the triangles when the bases DA, AQ are in a right line, and the inscribed circles equal to each other.

[4] XXIX. QUESTION, by Mr. Simon Woolcott.

REQUIRED the area of that curve whose equation is

$$y = \frac{ax}{\sqrt{a^2 - x^2}} + \frac{xx}{\sqrt{a^2 - x^2}}.$$

[5] XXX. QUESTION, by Mr. Tho. Todd.

SUPPOSE a gentleman to give his sons A and B equally between them, a pounds payable in 1 year, $2a$ in 2 years, $3a$ in 3 years and so on for ever: but the sons having agreed between themselves that A shall have the 1st annual payments, and B and his heirs shall have the rest after him: required x years the time in which A will receive his payments, allowing 5 per cent. per annum compound interest to both A and B.

[6] XXXI. QUESTION, by Mr. Benj. Hayson.

TO find the locus of the centers of an infinite number of circles touching two other circles given in magnitude and position.

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[7] XXXII. QUESTION, by Aumuneim.

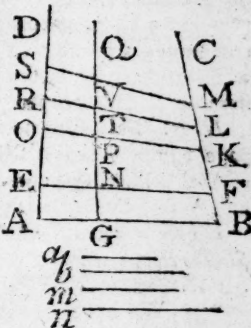
LET AB be a semicircle, BC a tang. thereto equal to the diam. AB , and let $CP, Cp, \&c.$ be lines drawn from C to meet the diam. AB in $P, p, \&c.$ also let $PQ, pq, \&c.$ be $\perp AB$, and meet the circumf. in $Q, q, \&c.$ and let $QE, qe, \&c.$ be drawn $\perp CP, Cp, \&c.$ and meet $CP, Cp, \&c.$ in $E, e, \&c.$ 'tis required to find the locus of the points $E, e, \&c.$

[8] XXXIII. QUESTION, by the late Mr. Will. Wilkin.

REQUIRED a general theorem for finding the sum of n terms of the following series, $1. 2^2. 3^3 + 3. 4^2. 5^3 + 5. 6^2. 7^3. + 7. 8^2. 9^3 + \&c.$

[9] XXXIV. QUESTION, by Mr. Tho. Moss.

IF the distance of two points A and B , and the position of the two indefinite lines AD and BC be given, and a right line EF be so drawn that the parts BF and AE may be in any assigned ratio of a to b ; and the two lines AB and EF be divided in G and N in the given ratio of m to n ; that is, AG to GB (and EN to NF) as m to n ; and let the indefinite line GNQ be drawn, and an indefinite number of points $K, L, M, \&c.$ and $O, R, S, \&c.$ be respectively taken in the lines BC and AD , such that BK may be to AO , BL to AR , and BM to $AS, \&c.$ always in the same given ratio of a to b (or BF to AE) and the lines OK, RL , and $SM, \&c.$ be drawn: then will these last mentioned lines be always divided by the line GNQ in the same given ratio of m to n ; that is, OP is to PK , RT to TL , and SV to $VM, \&c.$ in the given ratio AG to GB (or EN to NF) required a demonstration thereof from geometrical principles.



[10] XXXV. QUESTION, by the Rev. Mr. Lawfon.

GIVEN the vertical angle and the base, to determine the triangle when the rectangle of the sides is equal to the difference of their squares.

[11] XXXVI. QUESTION, by the Rev. Mr. Crakelt.

GIVEN the vertical angle, the difference of the base and one of the sides, and the perimeter; to construct the triangle.

[12] XXXVI. QUESTION, by Mr. George Sanderfon.

GIVEN the base, the difference of the sides, and the line bisecting the vertical angle of a plane triangle to construct it.

[13] XXXVII. QUESTION, by Mr. Isaac Dalby.

HAVING given two plane angles, it is required to find another plane angle, so that the three being joined, the two first may make a given solid angle.

[14]

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[14] XXXVIII. QUESTION, by Mr. Reuben Burrow.

HAVING two curves of any kind given in position, it is required to draw a line parallel to a line given in position, so that the part intercepted between the two curves may be of a given length.

[15] XXXIX. QUESTION, by Mr. George Beck.

SUPPOSE a triangle parallel to the horizon, and revolving equably in the direction of its plane, was to fall downwards, required the nature of the solid described thereby.

PRIZE QUESTION, by the Rev. Mr. Crakelt.

IF from one of the extremities of a given quadrant, four arches be taken in such a manner, that the difference of the two first arches, may be equal to the difference of the two last; then will the ratio of the tangents corresponding to the two first of the said arches be equal to, greater or less than, the ratio of the tangents corresponding to the two last arches, according as the first of the aforesaid differences is at the same, a greater or less distance from the middle of the quadrant, with or than the latter difference: Required the geometrical demonstration of this property.

N. B. This Question is, in effect, the same with that proposed on page 197 of *Maseres's Trigonometry*, the solution of which takes up several following pages in that work, and is at last given up as not to be effected by reasoning purely geometrical.

Whoever gives the best Solution to this Question before Candlemas-day, shall receive a Prize of Twelve Diaries, and the next best a Prize of Six Diaries.

*** We hope our ingenious Correspondents, will excuse any errors or omissions in this Diary, the Author being for some months past engaged on duty at Languard-Fort, and therefore unable to attend the publication, but intends in the next, to give additions and corrections to all the Errata in this, and the preceding Diaries.